



# Measurement of CP Violation in $B_s \rightarrow J/\psi\phi$ Decay at CDF

Gavril Giurgiu (for the CDF Collaboration)  
Johns Hopkins University

*Fermilab Wine and Cheese Seminar*  
*June 11, 2010*

# Introduction

- $CP$  violation means that the laws of nature are not invariant under the simultaneous transformation of Charge and Parity
- Charge conjugation transforms particles into anti-particles
- Parity transformation is a mirror reflection (space inversion)
- Parity conservation was first questioned by T.D. Lee and C.N. Yang in 1956 when they argued that there was no experimental evidence for parity conservation in weak interactions
- Same year, C.S. Wu showed that Parity is violated in beta decays of Cobalt nuclei
- The combined  $CP$  was soon adopted as the correct symmetry, just to be shown wrong by Cronin and Fitch in 1964 when they showed that  $CP$  is violated in neutral Kaon decays



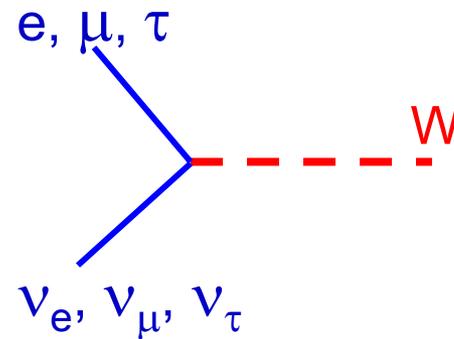
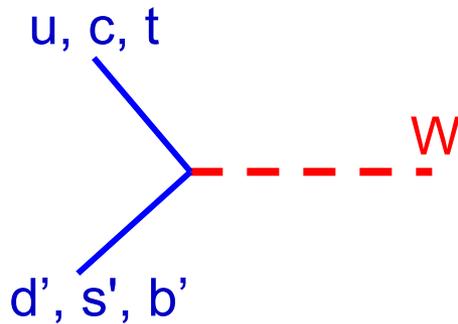
James Cronin



Val Fitch

## CP Violation in the Standard Model

- *CP* violation enters the Standard Model through complex phases in mixing matrices that connect up-type fermions with down-type fermions via *W* bosons:



$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

- Cabibbo-Kobayashi-Maskawa (CKM) quark mixing matrix transforms quark mass eigenstates into weak eigenstates and induces *CP* violation in the hadronic sector

- Pontecorvo-Maki-Nakagawa-Sakata (PMNS) neutrino mixing matrix  
→ induces neutrino oscillations and possibly *CP* violation in lepton sector

$$\begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{bmatrix}$$

# CKM Matrix

- Expand CKM matrix in  $\lambda = V_{us} = \sin(\theta_{Cabibbo}) \approx 0.23$

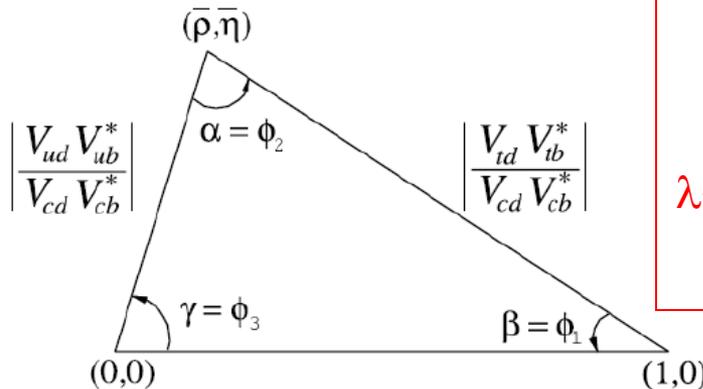
$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \approx \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda + \frac{1}{2}A^2\lambda^5[1 - 2(\rho + i\eta)] & 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4(1 + 4A^2) & A\lambda^2 \\ A\lambda^3[1 - (1 - \frac{1}{2}\lambda^2)(\rho + i\eta)] & -A\lambda^2 + \frac{1}{2}A\lambda^4[1 - 2(\rho + i\eta)] & 1 - \frac{1}{2}A^2\lambda^4 \end{pmatrix}$$

- To conserve probability CKM matrix must be unitary  
 → Unitary relations can be represented as “unitarity triangles”

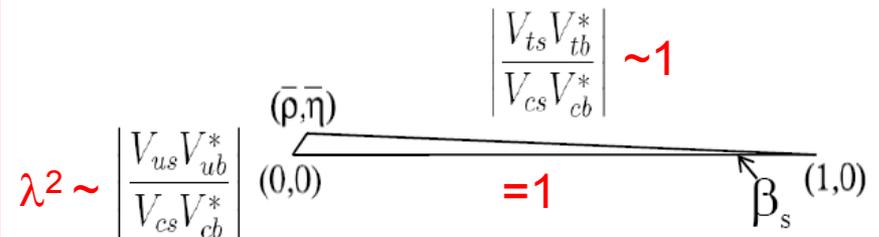
unitarity relations:

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

unitarity triangles:



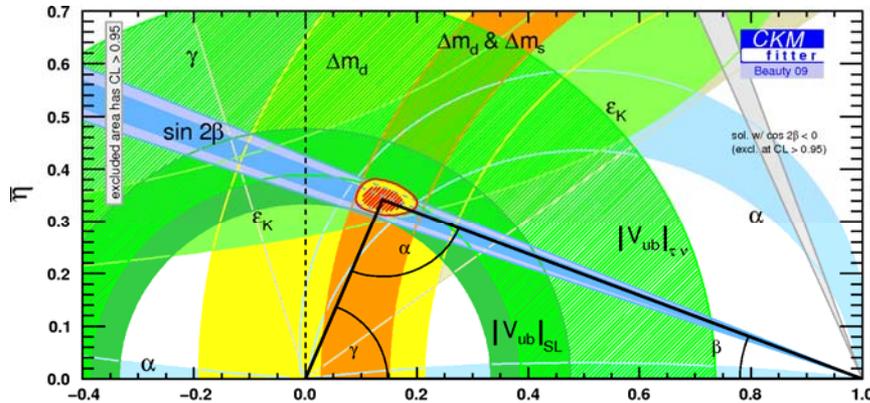
$$V_{us}V_{ub}^* + V_{cs}V_{cb}^* + V_{ts}V_{tb}^* = 0$$



Small  $CP$  violation phase  $\beta_s$  accessible in  $B_s \rightarrow J/\psi\Phi$  decays

## Why Look for CPV in $B_s$ System ?

- $CP$  violation has been studied in various Kaon and  $B$ -meson decays
- CKM matrix is well constrained by experimental data



- Within the SM framework,  $CP$  violation in the quark sector is too small to explain the matter - antimatter asymmetry in the universe
- Could still find large  $CP$  violation within the SM in the lepton sector
  - initial asymmetry between leptons and anti-leptons may induce baryon asymmetry through baryon number violation processes (lepto-genesis)
  - long baseline neutrino experiments will investigate  $CP$  violation in neutrino sector
- Alternatively we look for sources of  $CP$  violation beyond the SM in the quark sector
- Promising place to look for non-SM  $CP$  violation is the neutral  $B_s$  meson system

# Neutral $B_s$ System

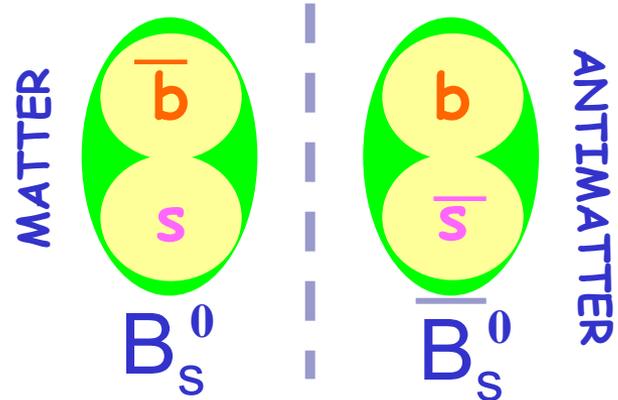
- Time evolution of  $B_s$  flavor eigenstates described by Schrodinger equation:

$$i \frac{d}{dt} \begin{pmatrix} |B_s^0(t)\rangle \\ |\bar{B}_s^0(t)\rangle \end{pmatrix} = \left( \mathbf{M} - \frac{i}{2} \mathbf{\Gamma} \right) \begin{pmatrix} |B_s^0(t)\rangle \\ |\bar{B}_s^0(t)\rangle \end{pmatrix}$$

- Diagonalize mass ( $M$ ) and decay ( $\Gamma$ ) matrices

→ mass eigenstates :

$$|B_s^H\rangle = p|B_s^0\rangle - q|\bar{B}_s^0\rangle \quad |B_s^L\rangle = p|B_s^0\rangle + q|\bar{B}_s^0\rangle$$



- Flavor eigenstates differ from mass eigenstates and mass eigenvalues are also different:

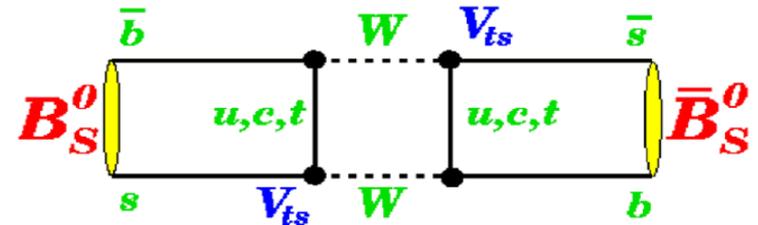
$$\Delta m_s = m_H - m_L \approx 2|M_{12}|$$

→  $B_s$  oscillates with frequency  $\Delta m_s$

precisely measured by

$$\text{CDF} \quad \Delta m_s = 17.77 \pm 0.12 \text{ ps}^{-1}$$

$$\text{DØ} \quad \Delta m_s = 18.56 \pm 0.87 \text{ ps}^{-1}$$

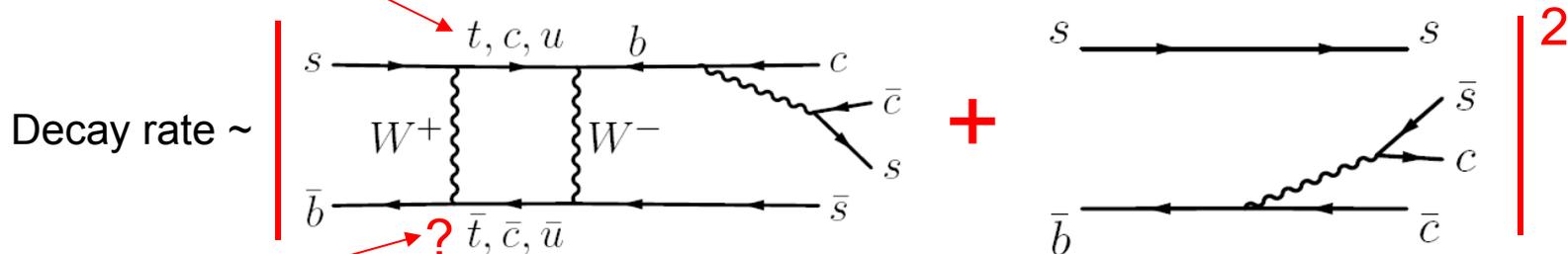
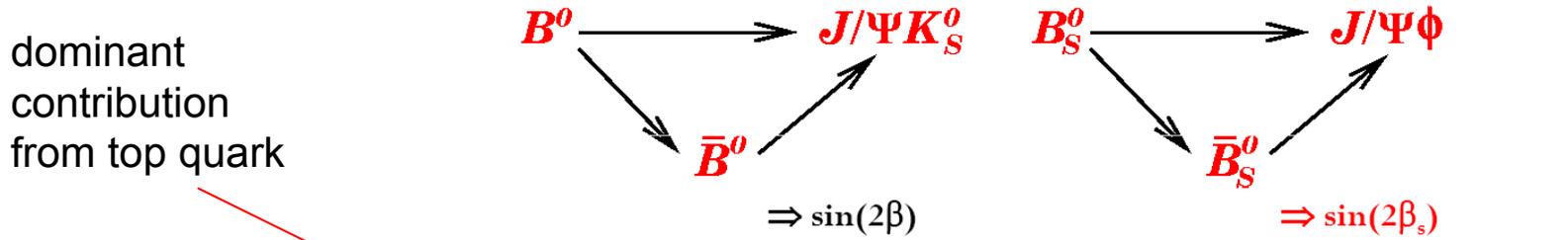


- Mass eigenstates have different decay widths

$$\Delta\Gamma = \Gamma_L - \Gamma_H \approx 2|\Gamma_{12}| \cos(\Phi_S) \quad \text{where} \quad \phi_s^{SM} = \arg\left(-\frac{M_{12}}{\Gamma_{12}}\right) \approx 4 \times 10^{-3}$$

# CP Violation in $B_s \rightarrow J/\psi\phi$ Decays

- Analogously to the neutral  $B^0$  system, CP violation in  $B_s$  system is accessible through interference of decays with and without mixing:



New Physics particles ?

$$\beta_s^{\text{SM}} = \arg(-V_{ts}V_{tb}^*/V_{cs}V_{cb}^*) \approx 0.02$$

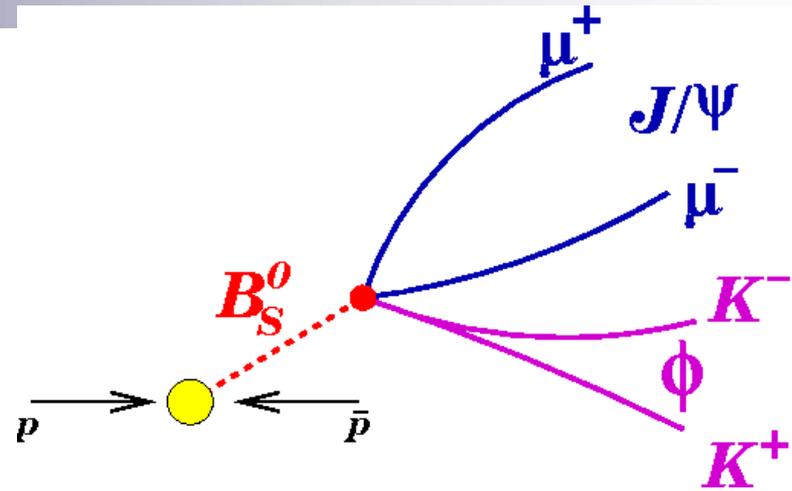
|          |          |          |
|----------|----------|----------|
| $V_{ud}$ | $V_{us}$ | $V_{ub}$ |
| $V_{cd}$ | $V_{cs}$ | $V_{cb}$ |
| $V_{td}$ | $V_{ts}$ | $V_{tb}$ |

- CP violation phase  $\beta_s$  in SM is predicted to be very small,  $O(\lambda^2)$
- New physics particles running in the mixing diagram may enhance  $\beta_s$ 
  - large  $\beta_s \rightarrow$  clear indication of New Physics !

# $B_s \rightarrow J/\psi \Phi$ Decays

- Measure:

- $B_s$  lifetime  $\tau_s$
- $B_{sH}, B_{sL}$  decay width difference  $\Delta\Gamma_s$
- $CP$  violating phase  $\beta_s$

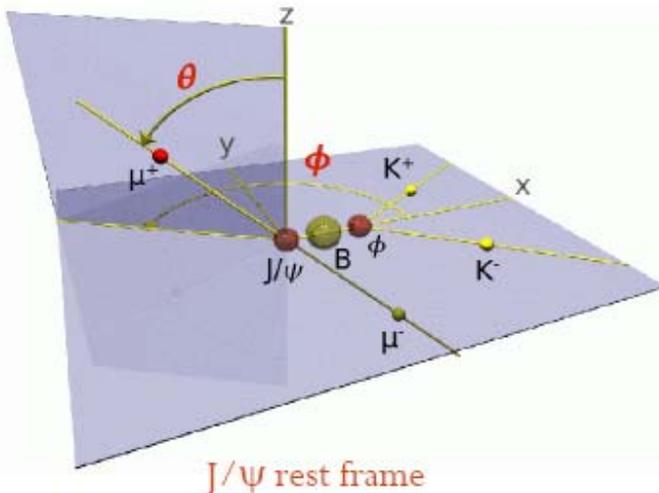


- Decay of  $B_s$  (spin 0) to  $J/\psi$  (spin 1) and  $\Phi$  (spin 1) leads to three different angular momentum final states:

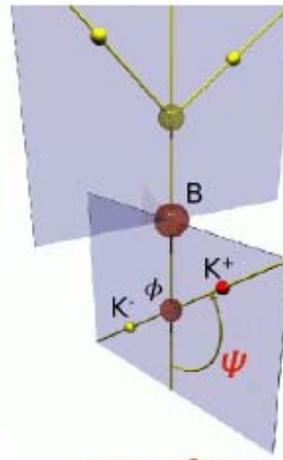
$L = 0$  (s-wave), 2 (d-wave)  $\rightarrow CP$  even (= short lived or light  $B_s$  if no  $CPV$ )

$L = 1$  (p-wave)

$\rightarrow CP$  odd (= long lived or heavy  $B_s$  if no  $CPV$ )



$J/\psi$  rest frame



$\Phi$  rest frame

- Three decay angles  $\vec{\rho} = (\theta, \phi, \psi)$  describe directions of final decay products  $\mu^+ \mu^- K^+ K^-$

# Transversity Basis

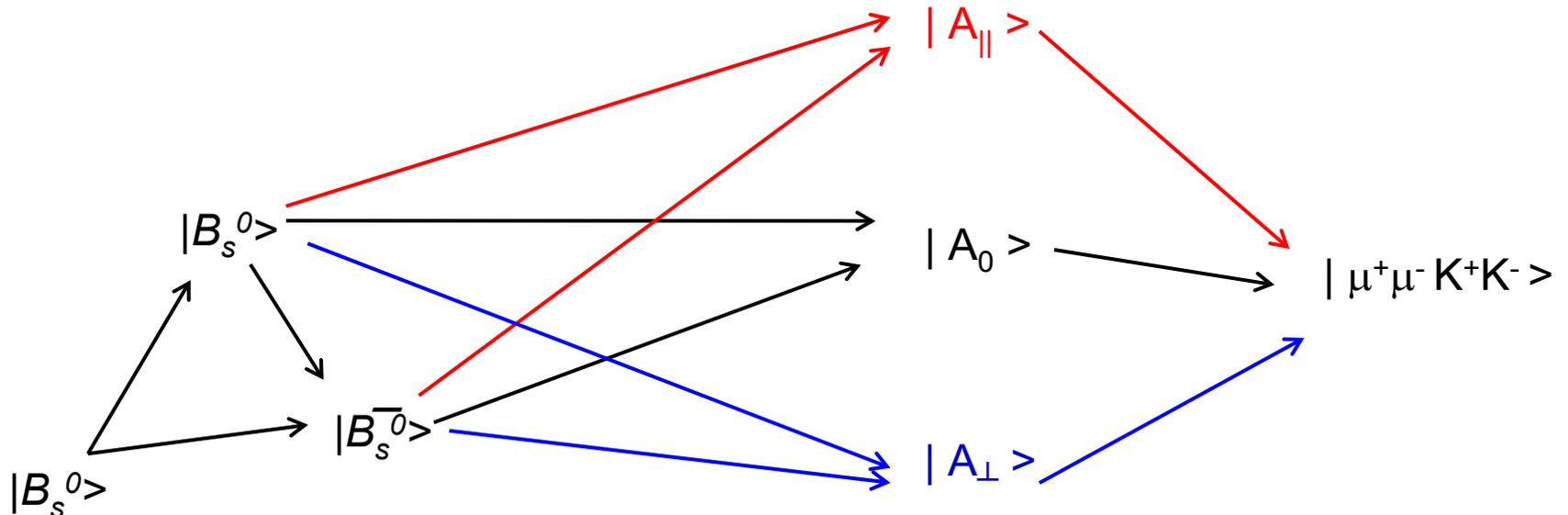
- Use “transversity basis” in which the vector meson polarizations w.r.t. direction of motion are either (Phys. Lett. B 369, 144 (1996), 184 hep-ph/9511363 ):

- transverse ( $\perp$  perpendicular to each other)  $\rightarrow$  *CP odd*

- transverse ( $\parallel$  parallel to each other)  $\rightarrow$  *CP even*

- longitudinal (0)  $\rightarrow$  *CP even*

- Corresponding decay amplitudes:  $A_0, A_{\parallel}, A_{\perp}$



# Decay Rate

-  $B_s \rightarrow J/\psi\phi$  decay rate as function of time, decay angles and initial  $B_s$  flavor:

$$\frac{d^4P(t, \vec{\rho})}{dt d\vec{\rho}} \propto |A_0|^2 \mathcal{T}_+ f_1(\vec{\rho}) + |A_{\parallel}|^2 \mathcal{T}_+ f_2(\vec{\rho})$$

$$+ |A_{\perp}|^2 \mathcal{T}_- f_3(\vec{\rho}) + |A_{\parallel}| |A_{\perp}| \mathcal{U}_+ f_4(\vec{\rho})$$

$$+ |A_0| |A_{\parallel}| \cos(\delta_{\parallel}) \mathcal{T}_+ f_5(\vec{\rho})$$

$$+ |A_0| |A_{\perp}| \mathcal{V}_+ f_6(\vec{\rho}),$$

time dependence terms

angular dependence terms

terms with  $\beta_s$  dependence

$$\mathcal{T}_{\pm} = e^{-\Gamma t} \times [\cosh(\Delta\Gamma t/2) \mp \cos(2\beta_s) \sinh(\Delta\Gamma t/2)$$

$$\mp \eta \sin(2\beta_s) \sin(\Delta m_s t)],$$

terms with  $\Delta m_s$  dependence present if initial state of B meson (B vs anti-B) is determined (flavor tagged)

$$\mathcal{U}_{\pm} = \pm e^{-\Gamma t} \times [\sin(\delta_{\perp} - \delta_{\parallel}) \cos(\Delta m_s t)$$

$$- \cos(\delta_{\perp} - \delta_{\parallel}) \cos(2\beta_s) \sin(\Delta m_s t)$$

$$\pm \cos(\delta_{\perp} - \delta_{\parallel}) \sin(2\beta_s) \sinh(\Delta\Gamma t/2)]$$

'strong' phases:

$$\mathcal{V}_{\pm} = \pm e^{-\Gamma t} \times [\sin(\delta_{\perp}) \cos(\Delta m_s t)$$

$$- \cos(\delta_{\perp}) \cos(2\beta_s) \sin(\Delta m_s t)$$

$$\pm \cos(\delta_{\perp}) \sin(2\beta_s) \sinh(\Delta\Gamma t/2)].$$

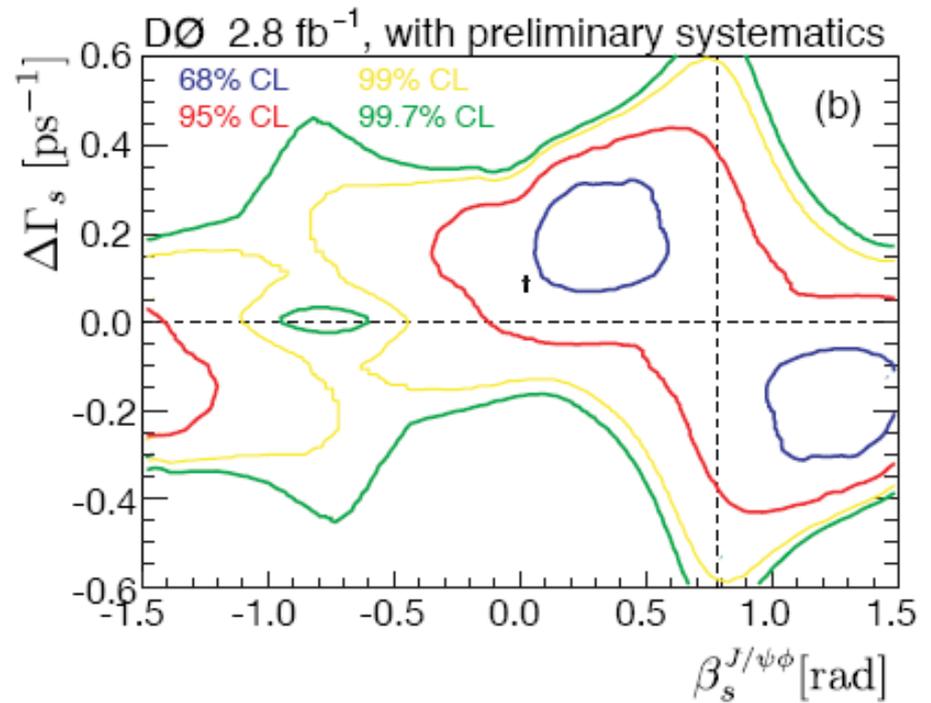
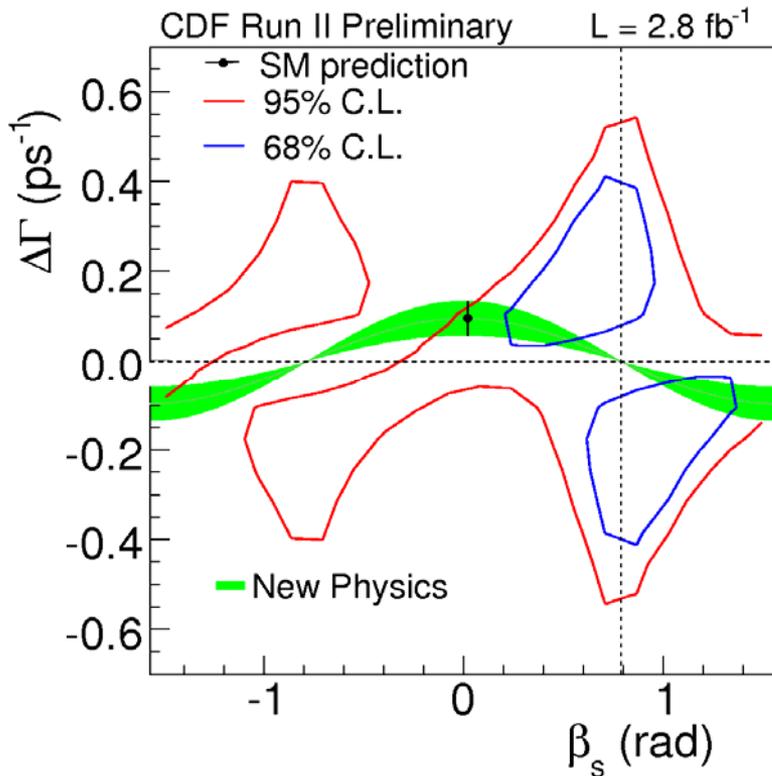
$$\delta_{\parallel} \equiv \text{Arg}(A_{\parallel}(0)A_0^*(0))$$

$$\delta_{\perp} \equiv \text{Arg}(A_{\perp}(0)A_0^*(0))$$

- Identification of  $B$  flavor at production (flavor tagging)  $\rightarrow$  better sensitivity to  $\beta_s$

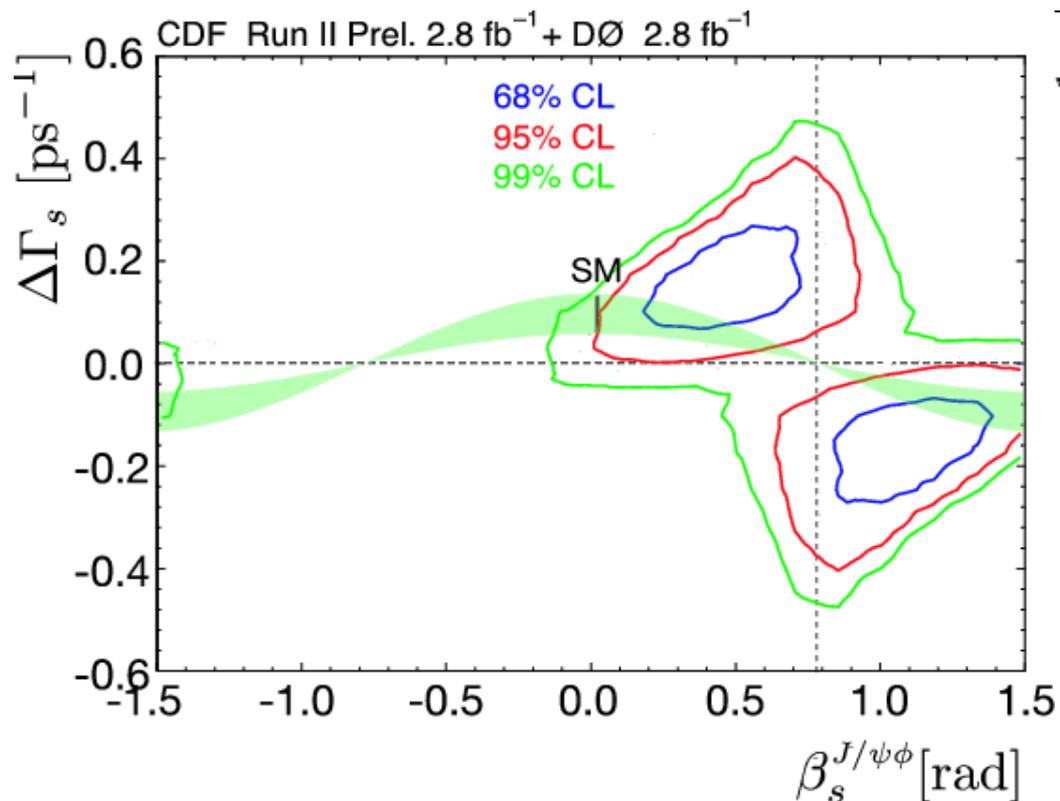
## Status Before This Update

- Both CDF (public note 9458) and DØ (conference Note 5933-CONF) showed  $\sim 1.5\sigma$  deviations from SM in the same direction



## Status Before This Update: CDF + DØ Combination

- CDF + DØ combination done by the Tevatron B Working Group:  
<http://tevbwg.fnal.gov/>
- Shows intriguing  $2.1\sigma$  deviation from SM expectation (CDF note 9787)



# CDF Detector

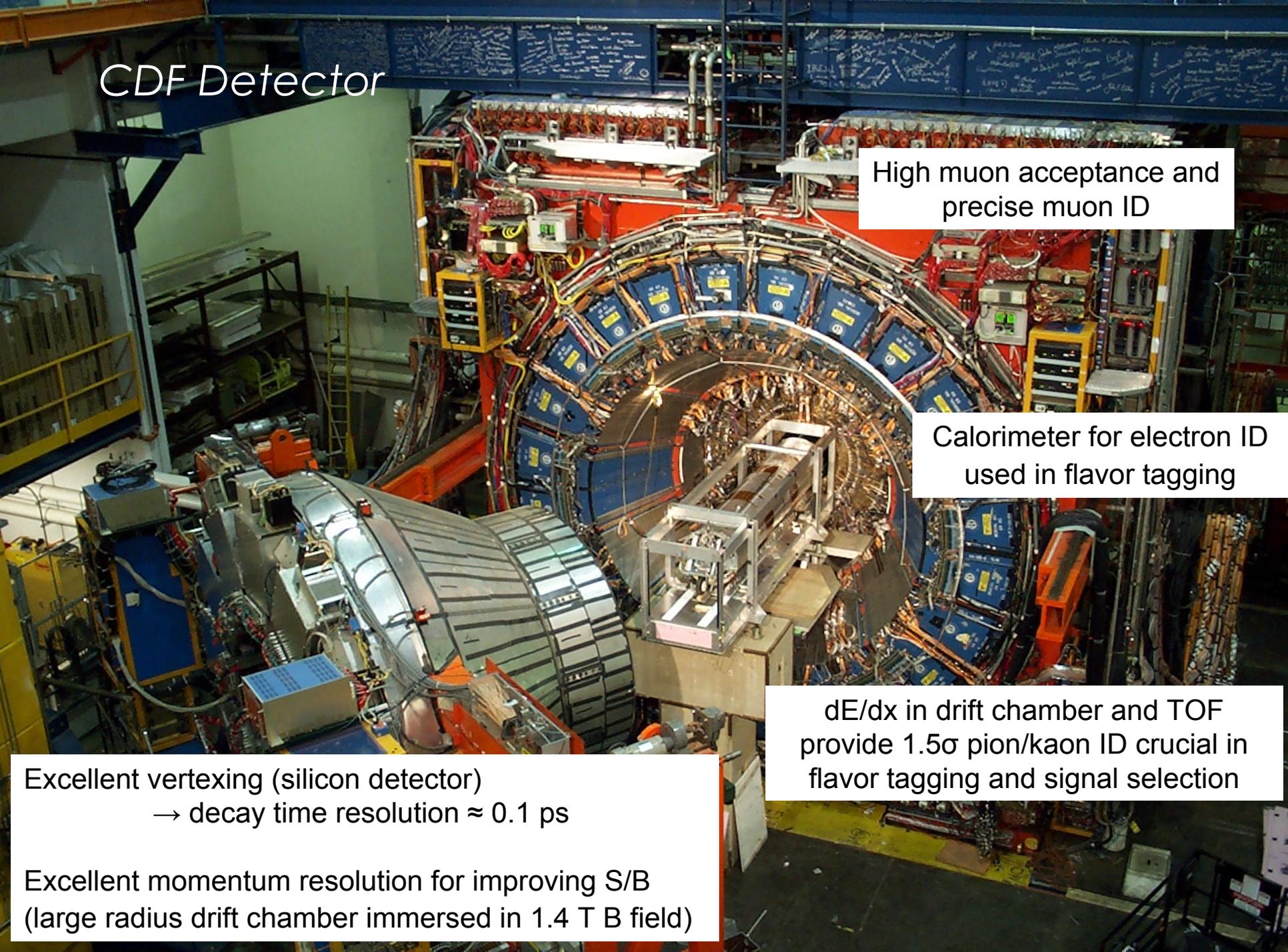
High muon acceptance and  
precise muon ID

Calorimeter for electron ID  
used in flavor tagging

$dE/dx$  in drift chamber and TOF  
provide  $1.5\sigma$  pion/kaon ID crucial in  
flavor tagging and signal selection

Excellent vertexing (silicon detector)  
→ decay time resolution  $\approx 0.1$  ps

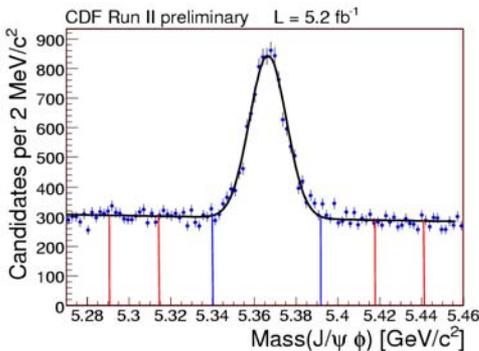
Excellent momentum resolution for improving S/B  
(large radius drift chamber immersed in 1.4 T B field)



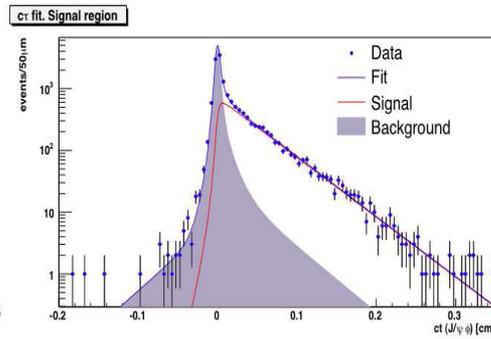
# Analysis Components

- Multi-dimensional likelihood fit

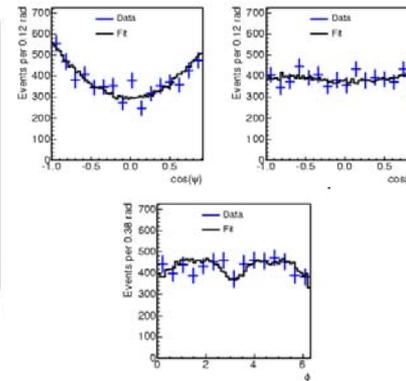
$$f_s P_s(m|\sigma_m) P_s(t, \vec{\rho}, \xi | \mathcal{D}, \sigma_t) P_s(\sigma_t) P_s(\mathcal{D})$$



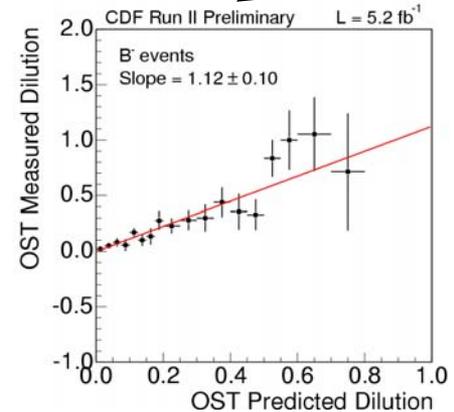
**Mass**  
discriminate signal  
against background



**Decay-time**  
determines lifetime  
of each mass  
eigenstate



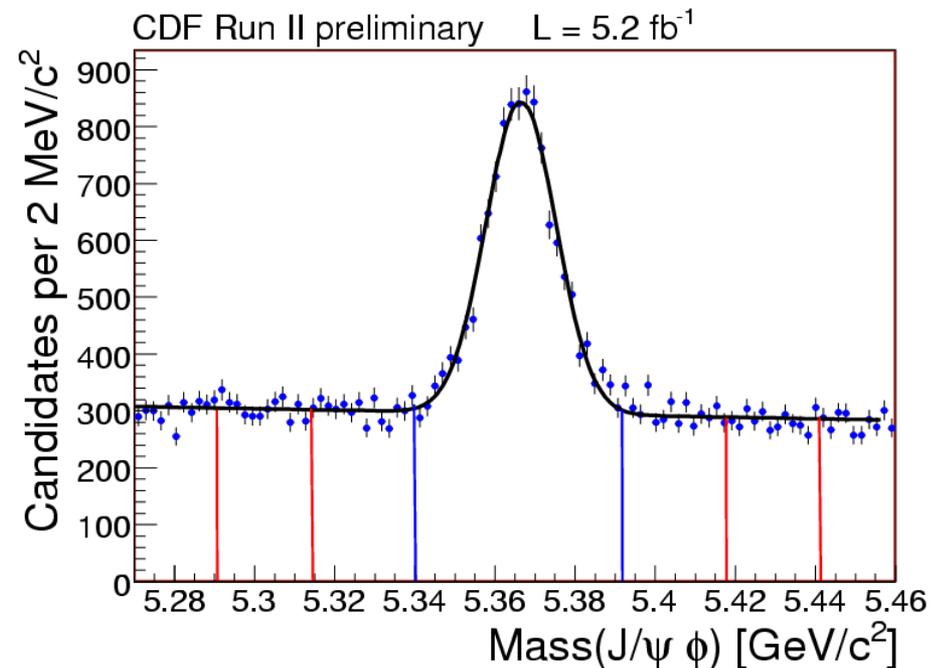
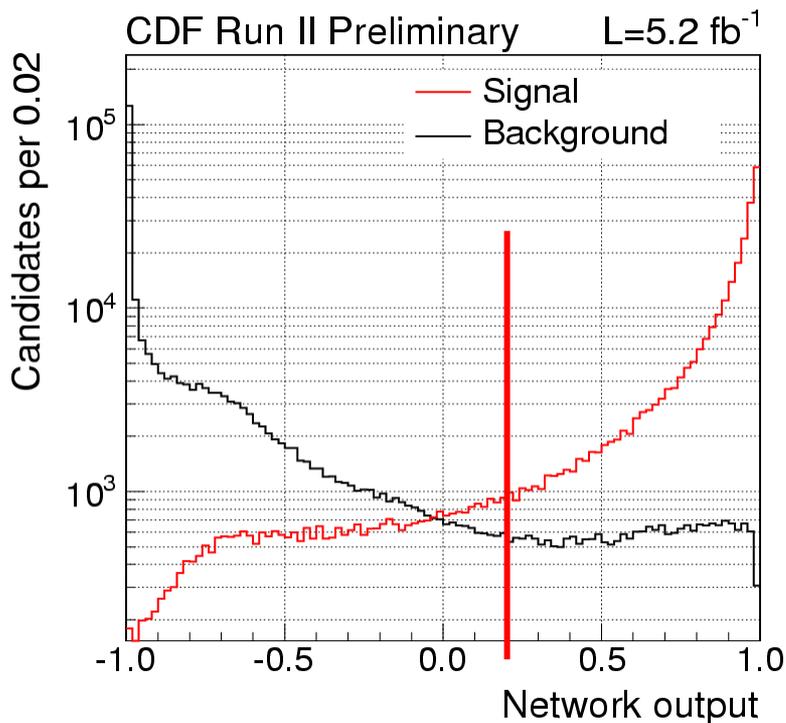
**Angles**  
separate CP-even  
from CP-odd final  
states



**Tagging**  
determines flavor  
of initial  $B_s$  state

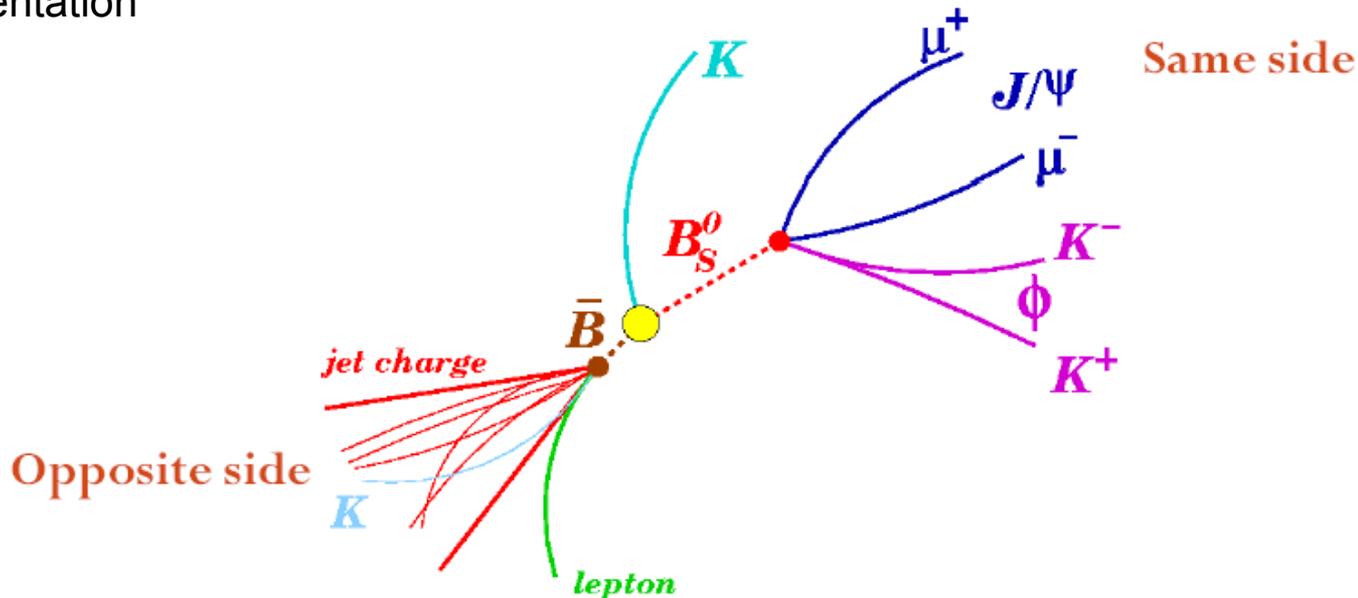
# Signal Reconstruction

- Reconstruct  $B_s^0 \rightarrow J/\psi \phi$  in  $5.2 \text{ fb}^{-1}$  of data from sample selected by di-muon trigger
- Combine kinematic variables with particle ID information (dE/dx, TOF) in neural network to discriminate signal from background
- Yield of  $\sim 6500$  signal  $B_s$  events with  $S/B \sim 1$  (compared to  $\sim 3150$  in  $2.8 \text{ fb}^{-1}$ )



# Flavor Tagging

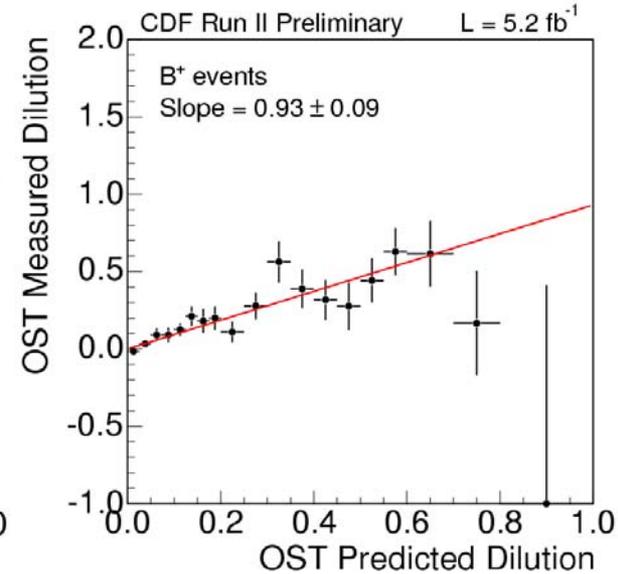
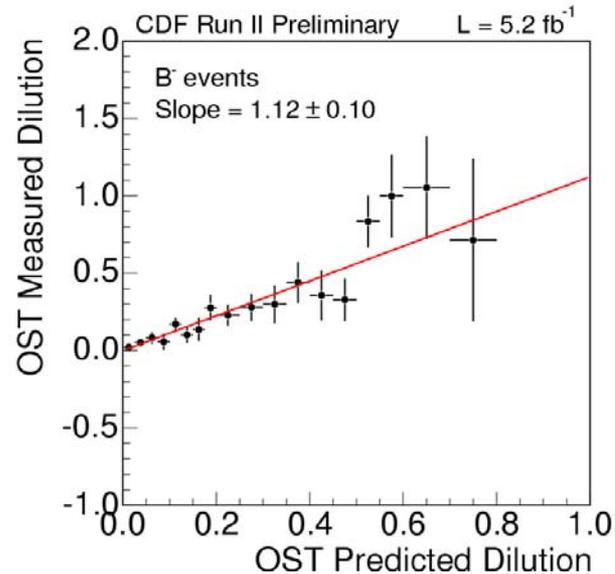
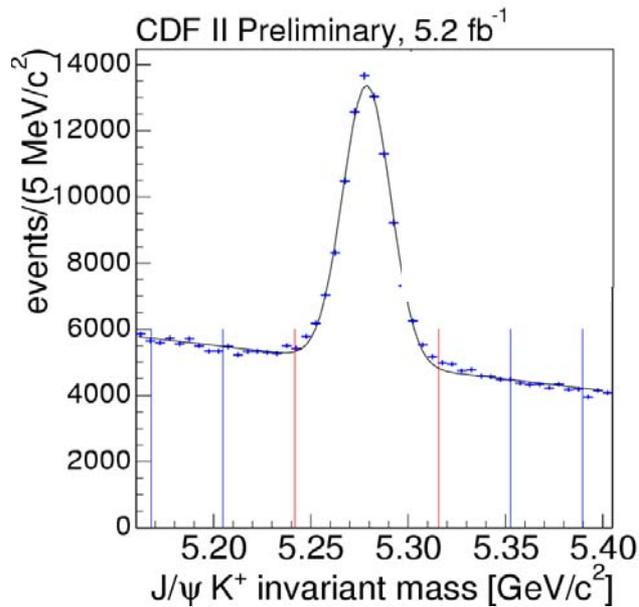
- Tevatron:  $b$ -quarks mainly produced in pairs of *bottom anti-bottom*
  - flavor of the  $B$  meson at production inferred with:
- Opposite Side Tagger (OST): exploits decay products of other  $b$ -hadron in the event
- Same Side Kaon Tagger (SSKT): exploits correlations with particles produced in fragmentation



- Output of flavor tagger:
  - flavor decision ( $b$ -quark or anti- $b$ -quark)
  - probability that the decision is correct:  $P = (1 + Dilution) / 2$

# Opposite Side Tagging Calibration and Performance

- OST combines in a NN opposite side lepton and jet charge information
- Initially calibrated using a sample of inclusive semileptonic  $B$  decays
  - predicts tagging probability on event-by-event basis
- Re-calibrated using  $\approx 52,000 B^{+/-} \rightarrow J/\psi K^{+/-}$  decays



- OST efficiency =  $94.2 \pm 0.4\%$ , OST dilution =  $11.5 \pm 0.2\%$  (correct tag probability  $\sim 56\%$ )
- Total tagging power =  $1.2\%$

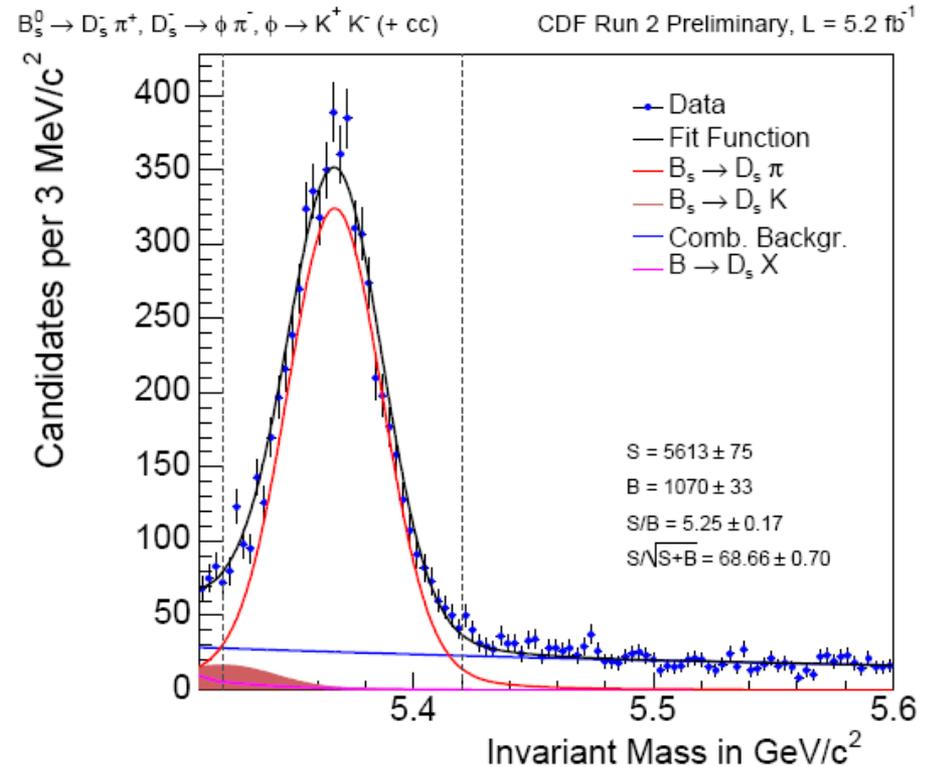
# Same Side Tagging Calibration

- Event-by-event predicted dilution based on simulation
- Calibrated with  $5.2 \text{ fb}^{-1}$  of data
- Simultaneously measuring the  $B_s$  mixing frequency  $\Delta m_s$  and the dilution scale factor  $A$

$$P_{Sig}(ct|\sigma_{ct}, \xi = \xi_D \cdot \xi_P, D) = \frac{1}{N} \cdot \left[ \frac{1}{\tau} e^{-\tilde{t}/\tau} \cdot (1 + \xi AD \cdot \cos(\Delta m_s \tilde{t})) \right] \otimes \mathcal{G}(\tilde{ct}|\sigma_{ct}) \cdot \epsilon(ct|\sigma_{ct})$$

- $D$  – event by event predicted dilution
- $\xi$  – tagging decision = +1, -1, 0 for  $B_s$ ,  $\bar{B}_s$  and un-tagged events
- Fully reconstructed  $B_s$  decays selected by displaced track trigger

| Decay Channel  | $S$                               |
|--|-----------------------------------|
| $B_s^0 \rightarrow D_s^- \pi^+, D_s^- \rightarrow \phi \pi^-$    | $5613 \pm 75$                     |
| $B_s^0 \rightarrow D_s^- \pi^+, D_s^- \rightarrow K^* K^-$       | $2761 \pm 53$                     |
| $B_s^0 \rightarrow D_s^- \pi^+, D_s^- \rightarrow (3\pi)^-$      | $2652 \pm 52$                     |
| $B_s^0 \rightarrow D_s^- (3\pi)^+, D_s^- \rightarrow \phi \pi^-$ | $1852 \pm 43$                     |
| <b>Sum</b>   | <b><math>12877 \pm 113</math></b> |



# Same Side Tagging Performance

-  $B_s$  oscillation frequency measured  $\Delta m_s = (17.79 \pm 0.07) \text{ ps}^{-1}$  (statistical error only)

- In good agreement with the published CDF measurement with  $1 \text{ fb}^{-1}$

PRL 97, 242003 2006, PRL 97, 062003 2006

$\Delta m_s = 17.77 \pm 0.10 \text{ (stat)} \pm 0.07 \text{ (syst)} \text{ ps}^{-1}$   
used as external constraint in  $\beta_s$  measurement

- Dilution scale factor (amplitude) in good agreement with 1:

$$A = 0.94 \pm 0.15 \text{ (stat.)} \pm 0.13 \text{ (syst.)}$$

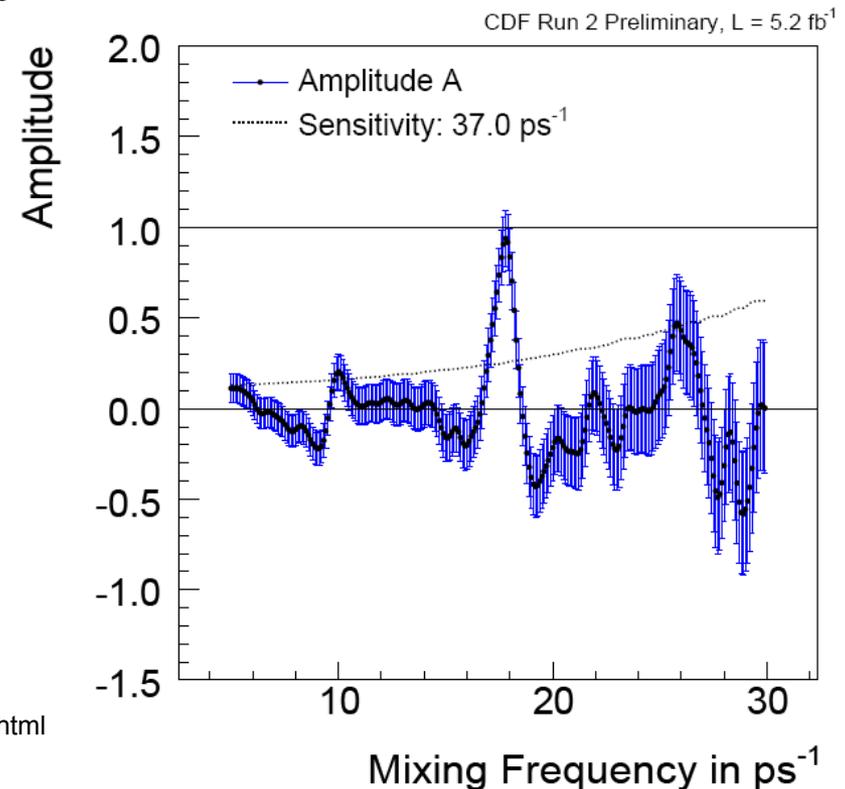
- Largest systematic uncertainty from decay time resolution modeling

- Total SSKT tagging power:

$$\varepsilon A^2 D^2 = (3.2 \pm 1.4) \%$$

<http://www-cdf.fnal.gov/physics/new/bottom/100204.blessed-sskt-calibration/index.html>

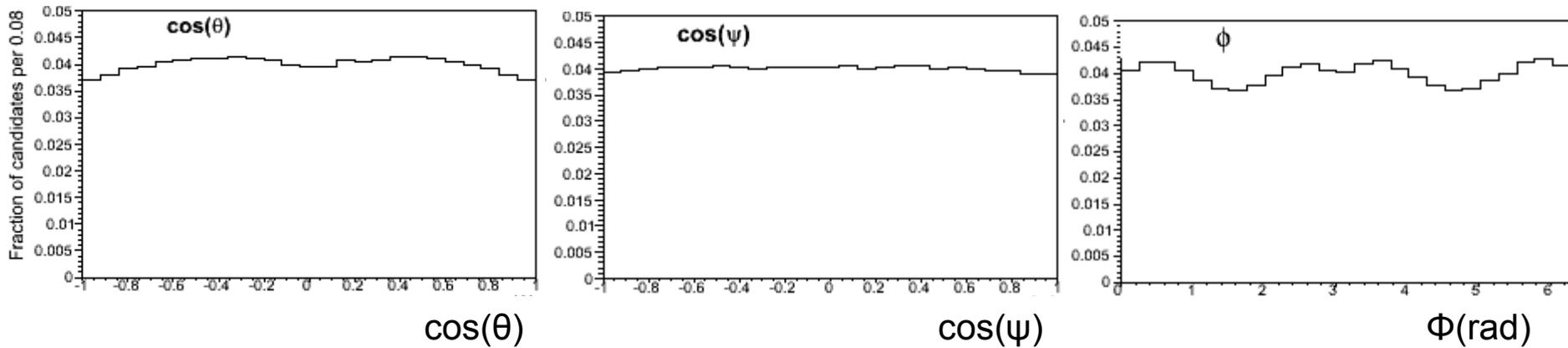
CDF public note 10108



# Detector Angular Efficiency

- *CP even* and *CP odd* final states have different angular distributions  
→ use angles  $\rho = (\theta, \phi, \psi)$  to statistically separate *CP even* and *CP odd* components
- Detector acceptance distorts the angular distributions  
→ determine 3D angular efficiency function from simulation and account for this effect in the fit

CDF Simulation of Detector Angular Sculpting



# $B_s$ Lifetime and Decay Width Difference

- Assuming no  $CP$  violation ( $\beta_s = 0$ ) obtain **most precise measurements of lifetime  $\tau_s$  and decay width difference  $\Delta\Gamma_s$** :

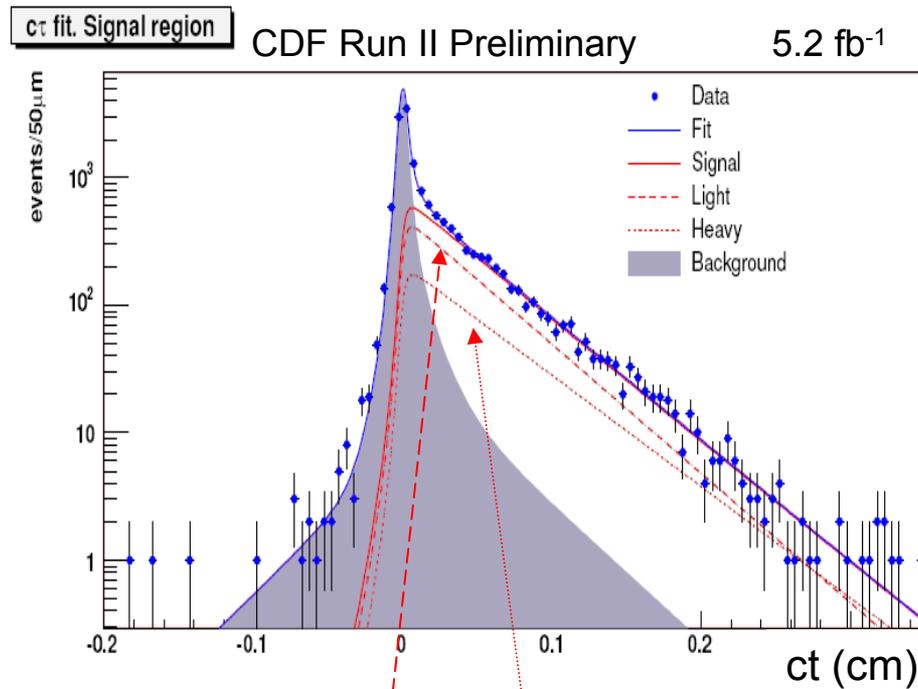
$$\tau_s = 1.53 \pm 0.025 \text{ (stat.)} \pm 0.012 \text{ (syst.) ps}$$

$$\Delta\Gamma = 0.075 \pm 0.035 \text{ (stat.)} \pm 0.01 \text{ (syst.) ps}^{-1}$$

compared to PDG 2009 averages:

$$\tau_s = 1.472^{+0.024}_{-0.026} \text{ ps}$$

$$\Delta\Gamma_s = 0.062^{+0.034}_{-0.037} \text{ ps}^{-1}$$



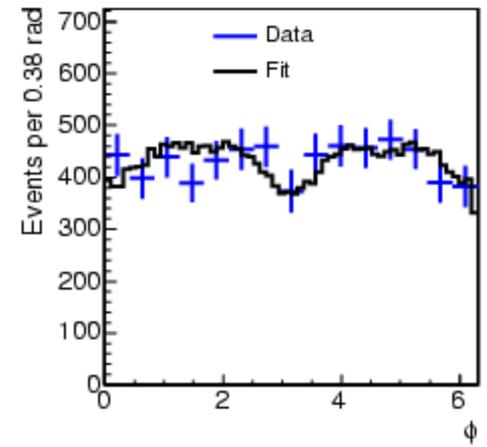
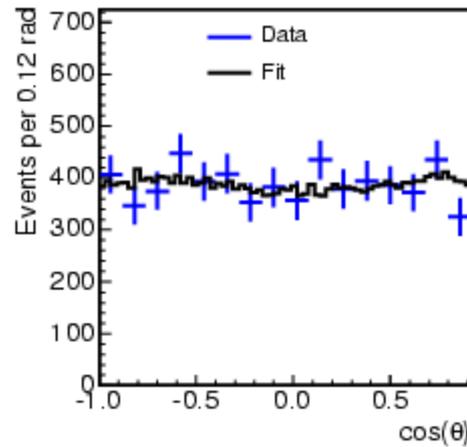
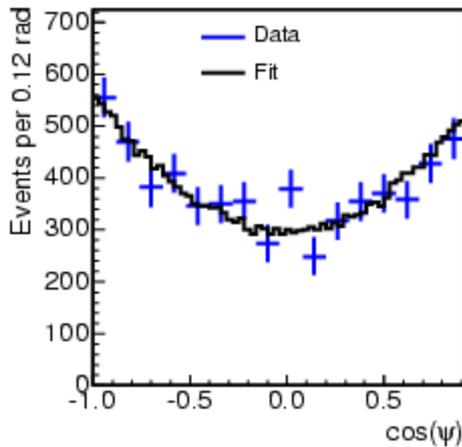
$CP$ -even ( $B_s^{light}$ ) and  $CP$ -odd ( $B_s^{heavy}$ ) components have different lifetimes  
 $\rightarrow \Delta\Gamma \neq 0$

# Polarization Amplitudes

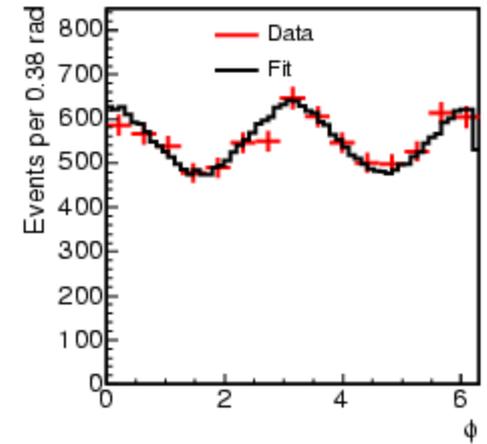
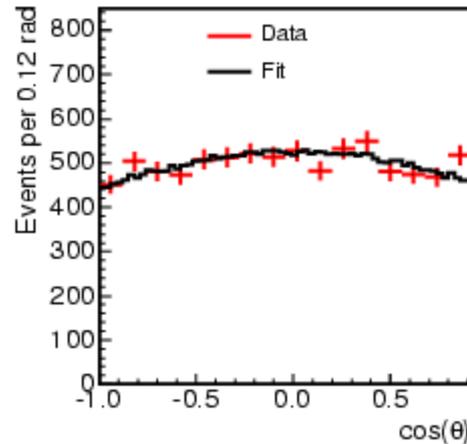
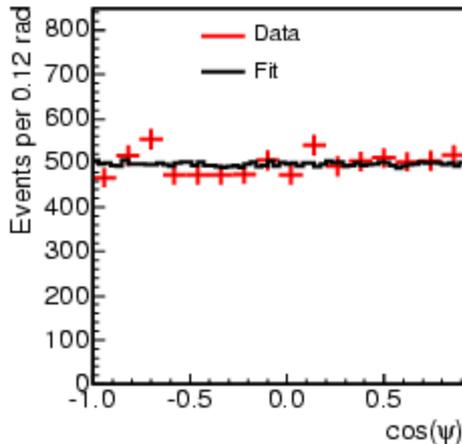
Most precise measurement of polarization amplitudes

$$|A_{\parallel}(0)|^2 = 0.231 \pm 0.014 \text{ (stat)} \pm 0.015 \text{ (syst.)}$$
$$|A_0(0)|^2 = 0.524 \pm 0.013 \text{ (stat)} \pm 0.015 \text{ (syst.)}$$
$$\phi_{\perp} = 2.95 \pm 0.64 \text{ (stat)} \pm 0.07 \text{ (syst.)}$$

Signal fit projections



Background fit projections

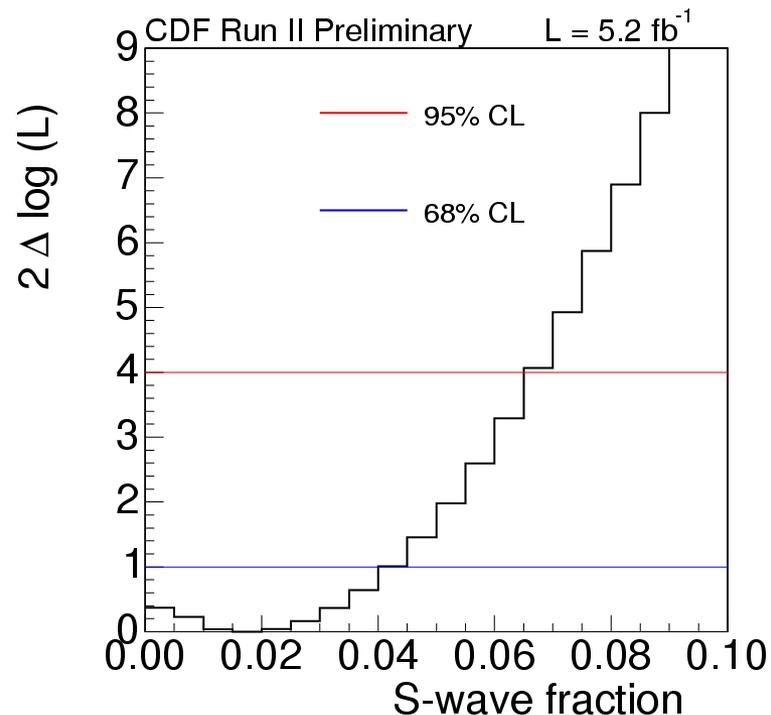


## S-Wave

- As noted in [arxiv:0812.2832v3](#), the  $KK$  pair in  $B_s \rightarrow J/\psi KK$  decays can be in an s-wave state with  $\sim 6\%$  contribution in a  $\pm 10$  MeV window around the  $\phi$  peak
- Systematic effects from neglecting such contribution were first investigated by [Clarke et al](#) in [arxiv:0908.3627v1](#) where it is shown that:
  - 10% un-accounted s-wave contamination in the  $\phi$  region leads to
    - 10% bias in the measured  $2\beta_s$ , towards the SM prediction
    - 15% increase in statistical errors
- S-wave contribution can be either non-resonant or from the  $f^0(980)$  resonance
- To account for potential s-wave contribution, enhance the likelihood function to account for the s-wave amplitude  $A_S$  and interference between s-wave and p-wave
- Time dependence of the s-wave amplitude  $A_S$  is *CP-odd*, same as  $A_\perp$
- Mass and phase of s-wave component are assumed flat (good approximation in a narrow  $\pm 10$  MeV around the  $\phi$  mass)

# S-Wave Measurement

- The fitted s-wave fraction is found to be very small in the KK mass range used in this analysis: [1.009, 1.028] GeV  
s-wave fraction < 6.7% at 95% C.L.
- To be compared with expectation from [arxiv:0812.2832v3](#) of 6.3% s-wave contribution in a range of +/- 10 MeV around the  $\Phi$  peak



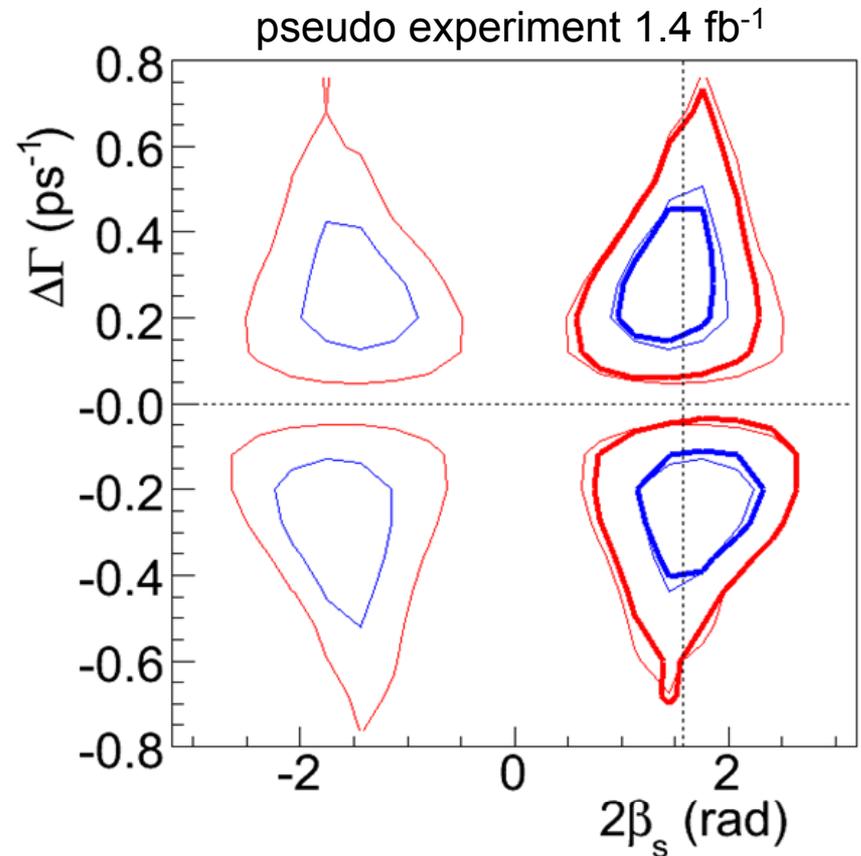
# CP Violation Phase $\beta_s$ in Tagged $B_s \rightarrow J/\psi\Phi$ Decays

- Without the s-wave the likelihood function is symmetric under the transformation

$$2\beta_s \rightarrow \pi - 2\beta_s \quad \Delta\Gamma \rightarrow -\Delta\Gamma$$

$$\delta_{\parallel} \rightarrow 2\pi - \delta_{\parallel} \quad \delta_{\perp} \rightarrow \pi - \delta_{\perp}$$

- Study expected effect of tagging using pseudo-experiments
- Improvement of parameter resolution is small due to limited tagging power ( $\epsilon D^2 \sim 4.5\%$  compared to B factories  $\sim 30\%$ )
- However,  $\beta_s \rightarrow -\beta_s$  no longer a symmetry  $\rightarrow$  4-fold ambiguity reduced to 2-fold ambiguity
- Adding the s-wave “slightly” breaks the symmetry due to asymmetric  $\Phi$  mass shape
- Symmetry still valid with good approximation...



$$2\Delta\log(L) = 2.3$$

$$2\Delta\log(L) = 6.0$$

— un-tagged

— tagged

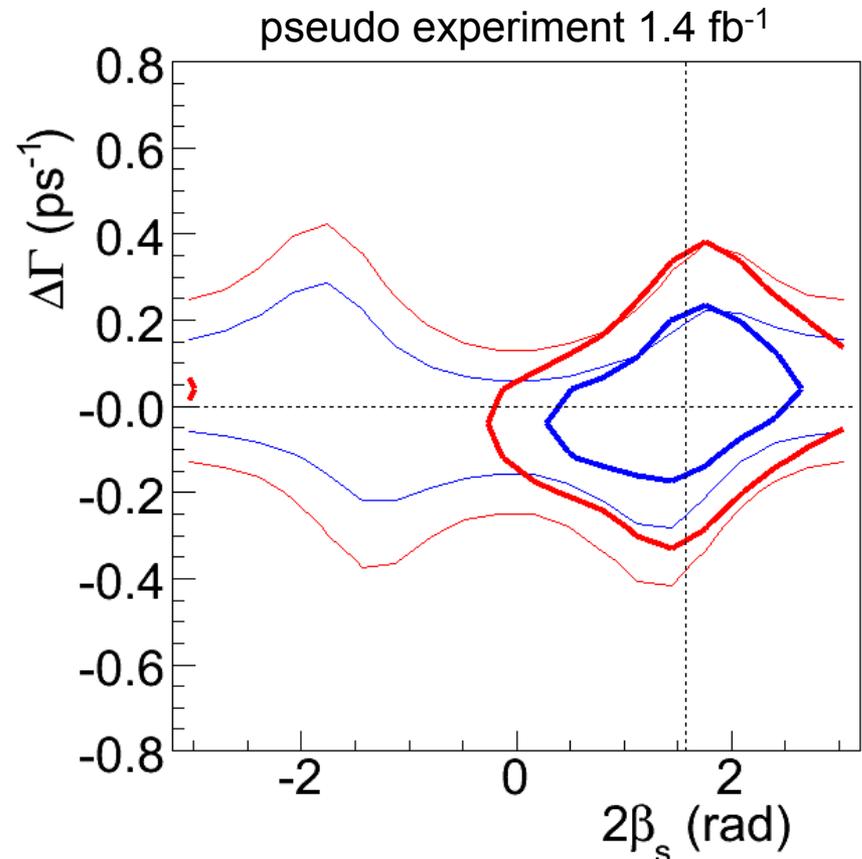
# CP Violation Phase $\beta_s$ in Tagged $B_s \rightarrow J/\psi\Phi$ Decays

- Without the s-wave the likelihood function is symmetric under the transformation

$$2\beta_s \rightarrow \pi - 2\beta_s \quad \Delta\Gamma \rightarrow -\Delta\Gamma$$

$$\delta_{\parallel} \rightarrow 2\pi - \delta_{\parallel} \quad \delta_{\perp} \rightarrow \pi - \delta_{\perp}$$

- Study expected effect of tagging using pseudo-experiments
- Improvement of parameter resolution is small due to limited tagging power ( $\epsilon D^2 \sim 4.5\%$  compared to B factories  $\sim 30\%$ )
- However,  $\beta_s \rightarrow -\beta_s$  no longer a symmetry  $\rightarrow$  4-fold ambiguity reduced to 2-fold ambiguity
- Adding the s-wave “slightly” breaks the symmetry due to asymmetric  $\Phi$  mass shape
- Symmetry still valid with good approximation



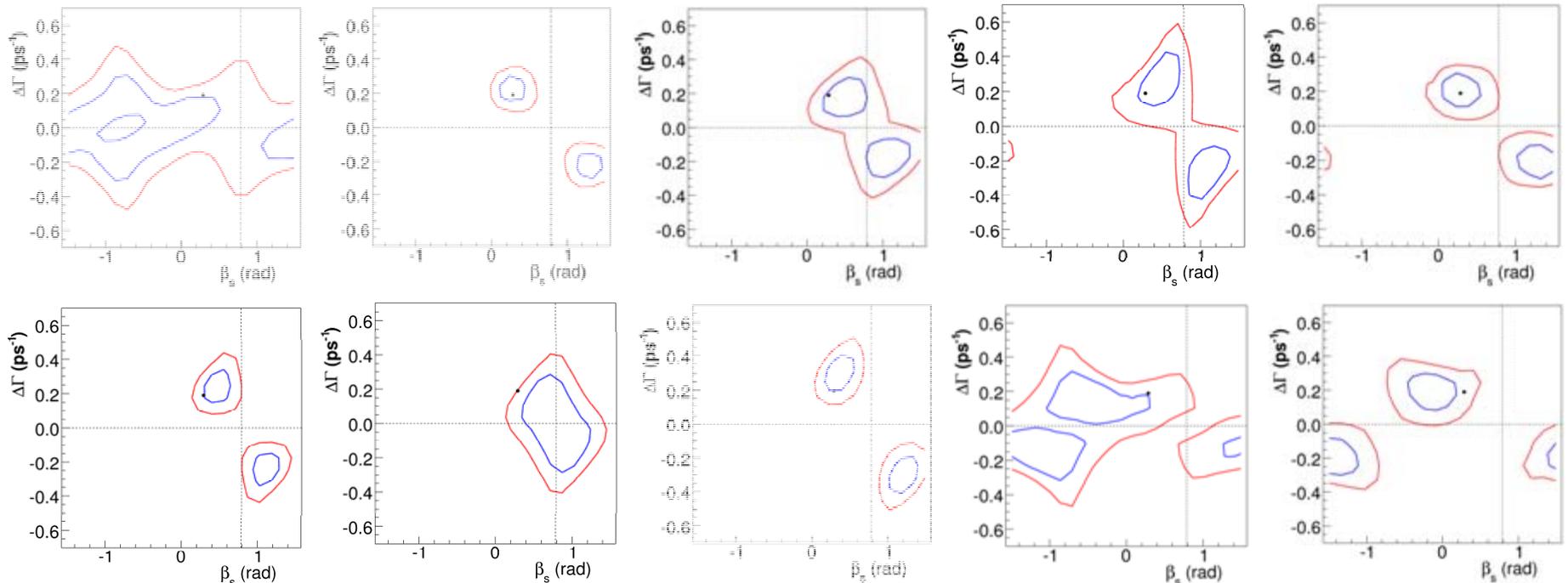
$2\Delta\log(L) = 2.3$  — un-tagged  
 $2\Delta\log(L) = 6.0$  — tagged

# Cross Checks With Pseudo-Experiments

- Generate 10 pseudo-experiments with  $\beta_s = 0.3$  and  $\Delta\Gamma = 0.2$  corresponding to  $1.4 \text{ fb}^{-1}$ 
  - same parameters, just different random seeds
- Large fluctuations expected in shape and size of confidence regions

—  $2\Delta\log(L) = 2.3$

—  $2\Delta\log(L) = 6.0$



# Non-Gaussian Regime

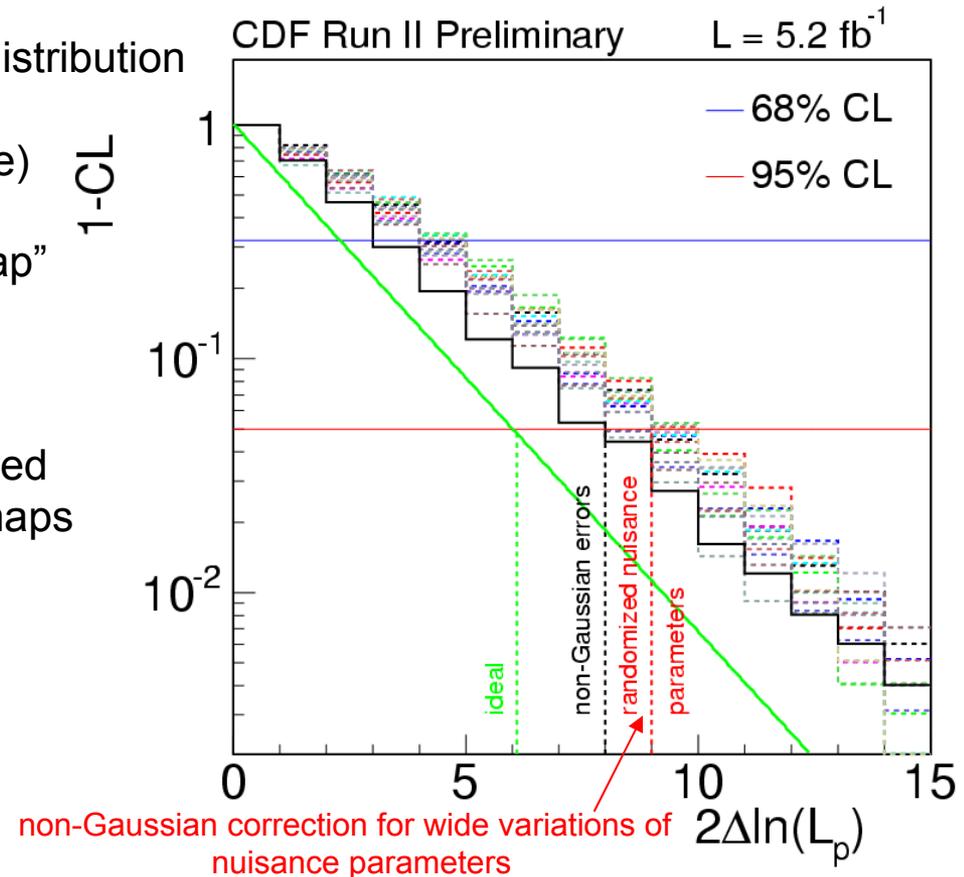
- Pseudo-experiments show that we are still not in perfect Gaussian regime  
→ *quote confidence regions instead of point estimates*
- In ideal case (high statistics, Gaussian likelihood), to get the 2D 68% (95%) C.L. regions, take a slice through profiled likelihood at 2.3 (6.0) units up from minimum

- In this analysis integrated likelihood ratio distribution (black histogram) deviates from the ideal  $\chi^2$  distribution (green continuous curve)

- Using pseudo-experiments establish a “map” between Confidence Level and  $2\Delta\log(L)$

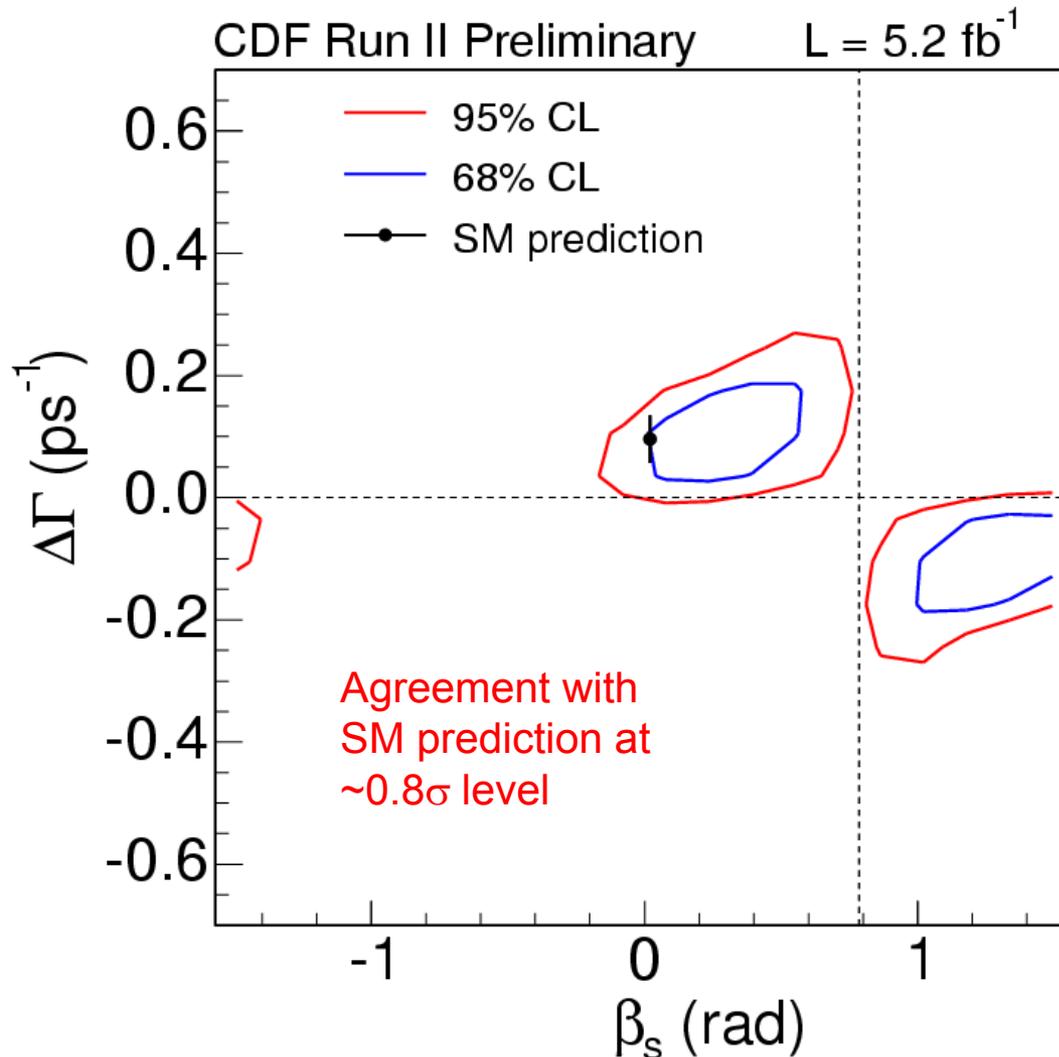
- All nuisance parameters are randomly varied within  $\pm 5\sigma$  from their best fit values and maps of CL vs  $2\Delta\log(L)$  re-derived

- To establish final confidence regions use most conservative case



# CP Violation Phase $\beta_s$ with $5.2 \text{ fb}^{-1}$ at CDF

- Final confidence regions in  $\beta_s$ - $\Delta\Gamma_s$  space:

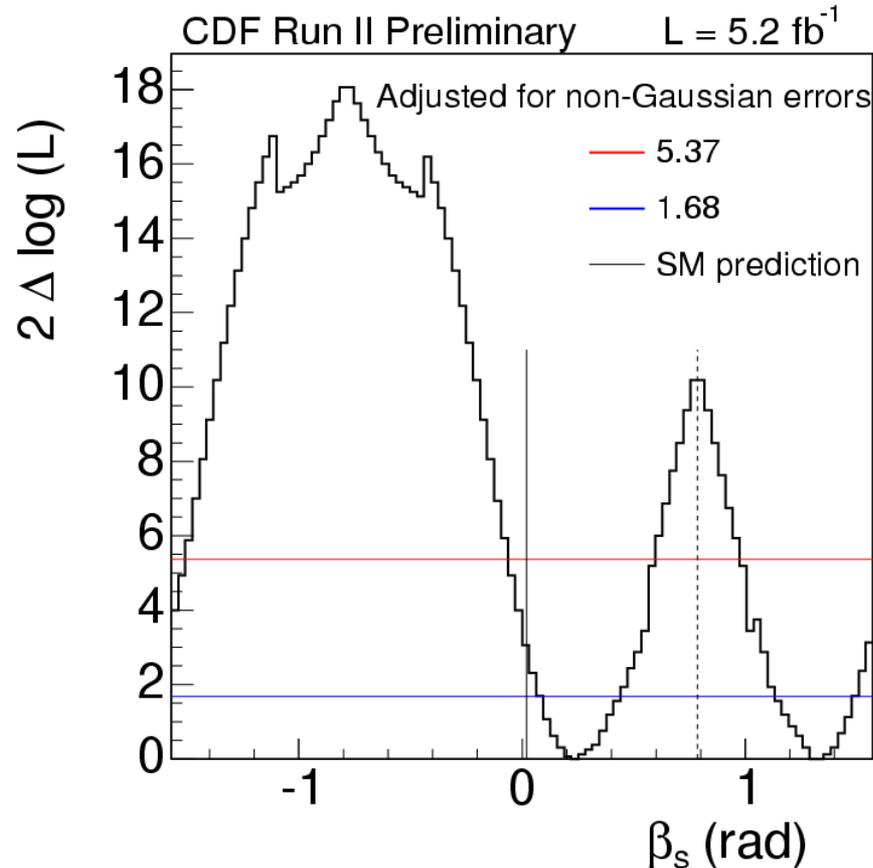


# 1D Profiled Likelihood for $\beta_s$

- CP violation phase  $\beta_s$  is bounded by the ranges:

$[0.02, 0.52] \cup [1.08, 1.55]$  at 68% C.L.

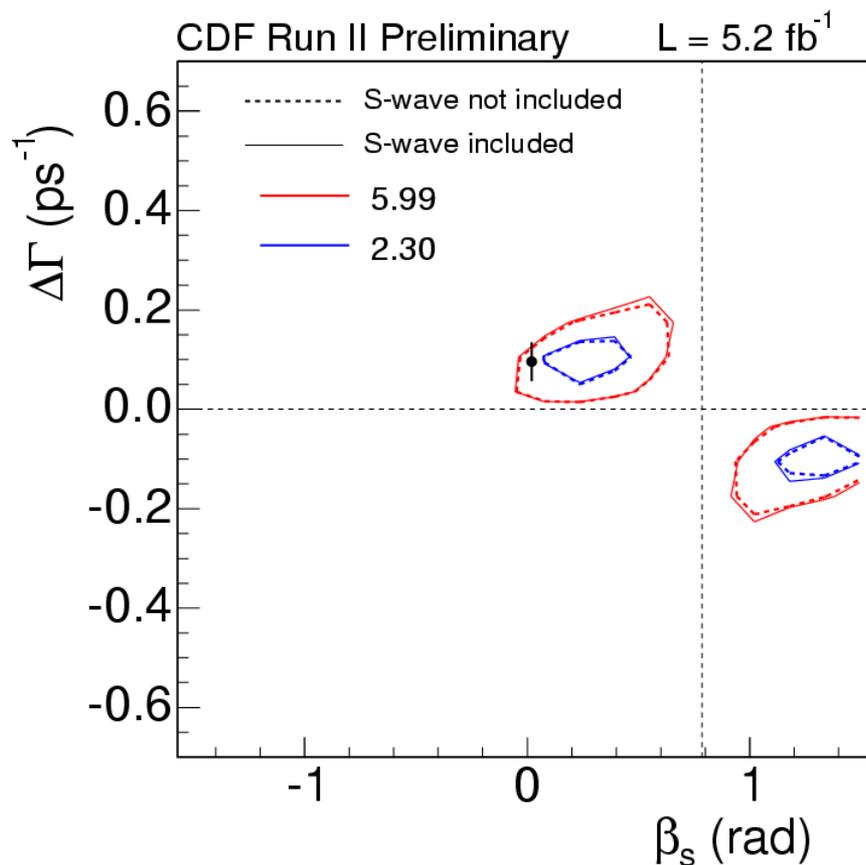
$[-\pi/2, -1.44] \cup [-0.13, 0.68] \cup [0.89, \pi/2]$  at 95% CL



Agreement with SM at  $\sim 1\sigma$  level

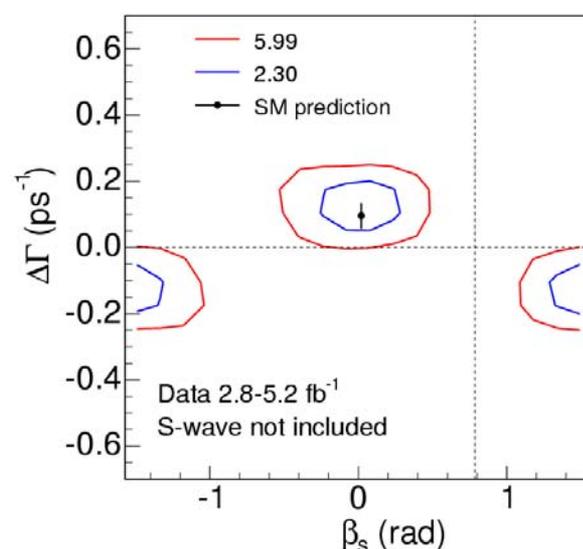
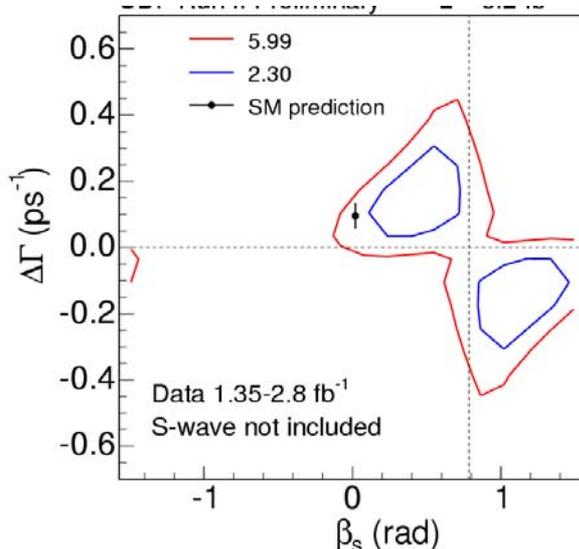
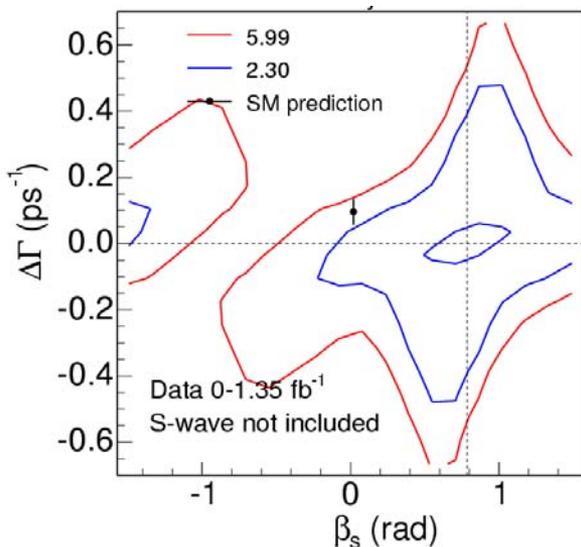
## $\beta_s$ - $\Delta\Gamma$ Contours with and without Including the S-Wave

- Compare likelihood contours with and without including the s-wave
- Very small effect on  $\beta_s$  and  $\Delta\Gamma$



# Comparison Between Different Data Periods

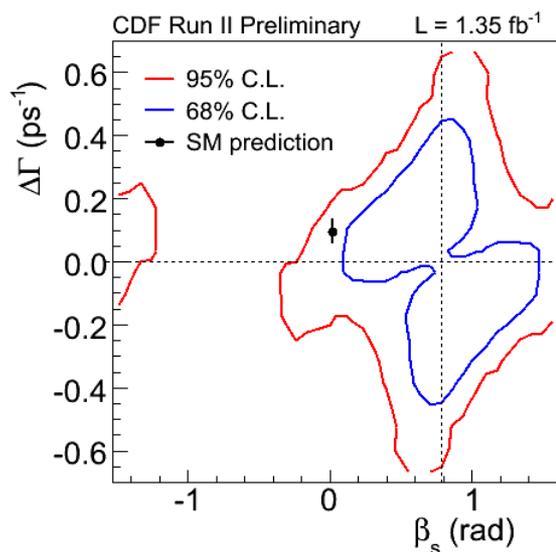
- Divide  $5.2 \text{ fb}^{-1}$  sample in three sub-samples corresponding to three public releases:
  - 0 -  $1.4 \text{ fb}^{-1}$  (initial result released at the end of 2007, PRL 100, 161802 (2008), arXiv:0712.2397)
  - 1.4 -  $2.8 \text{ fb}^{-1}$  (added for 2008 ICHEP update)
  - 2.8 -  $5.2 \text{ fb}^{-1}$  (added for this update)
- Previous results reproduced with updated analysis
- Clearly, improved agreement with the SM expectation comes from the second half of data ( $2.8 - 5.2 \text{ fb}^{-1}$ )



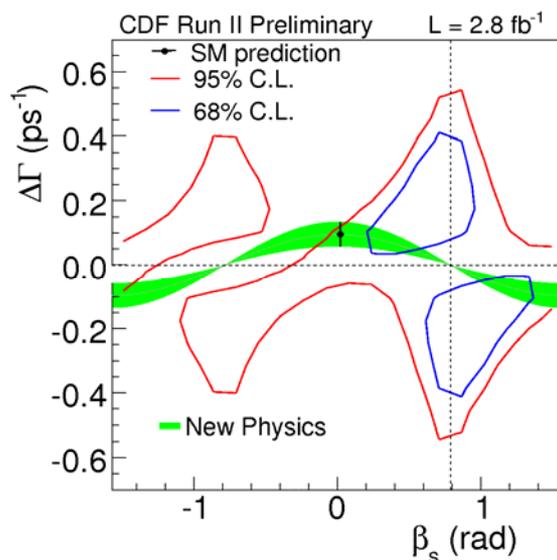
# Comparison with Previous Results

- $\beta_s$  and  $\Delta\Gamma_s$  allowed parameter space greatly reduced
- Agreement with SM expectation improves with higher statistics

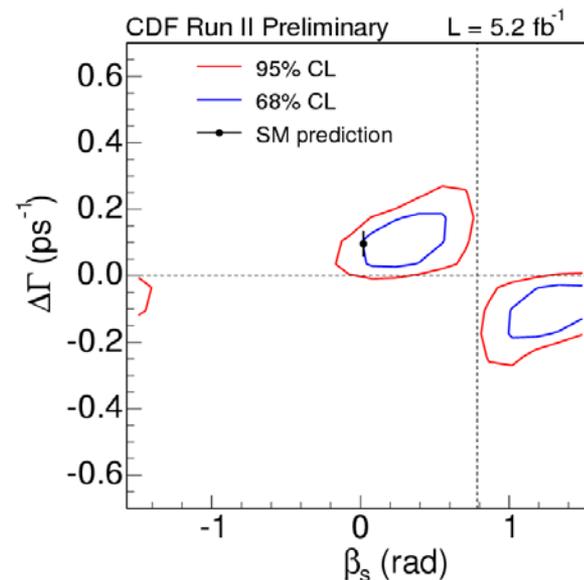
Initial result released at the end of 2007, PRL 100, 161802 (2008)  
arXiv:0712.2397  
~2000 signal events



2008 ICHEP update with preliminary PID and tagging  
~3150 signal events



**This update**  
**~6500 signal events**



## Conclusions

- Measurement of CP violation in  $B_s$  system updated by CDF with  $5.2 \text{ fb}^{-1}$
- Tightened constraints in  $\beta_s$  space:  
 *$[0.02, 0.52] \cup [1.08, 1.55]$  at 68% C.L.*
- Improved agreement with SM expectation, at  $\sim 1\sigma$  level
- Best measurements of  $B_s$  lifetime, decay width difference  $\Delta\Gamma_s$  and polarization amplitudes

$$c\tau_s = 458.7 \pm 7.5 \text{ (stat)} \pm 3.6 \text{ (syst)} \mu\text{m}$$

$$\Delta\Gamma_s = 0.075 \pm 0.035 \text{ (stat)} \pm 0.01 \text{ (syst)} \text{ ps}^{-1}$$

$$|A_{||}(0)|^2 = 0.231 \pm 0.014 \text{ (stat)} \pm 0.015 \text{ (syst)}$$

$$|A_0(0)|^2 = 0.524 \pm 0.013 \text{ (stat)} \pm 0.015 \text{ (syst)}.$$

# Prospects

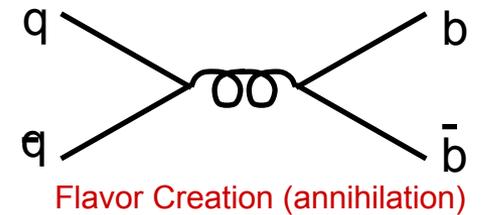
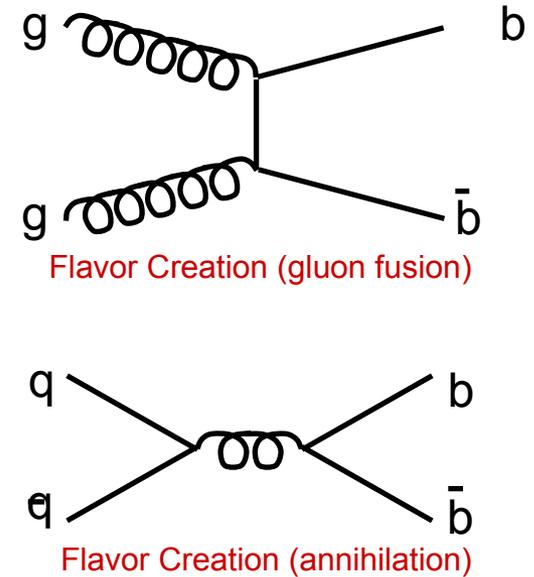
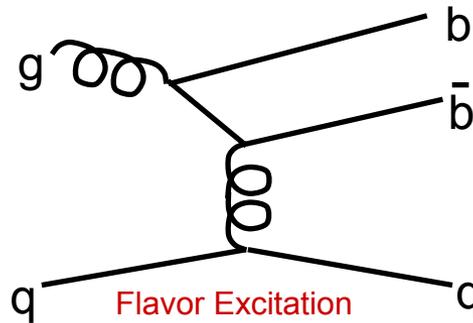
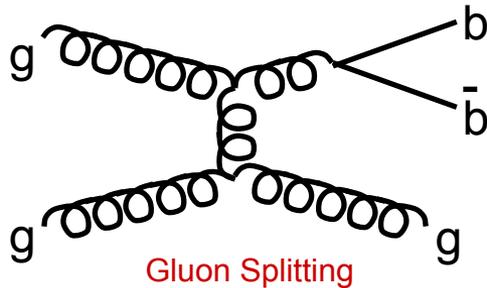
- Possible analysis improvements:
  - Improve statistics by ~25-30% by adding  $B_s \rightarrow J/\psi\phi$  decays from displaced track trigger (difficult due to trigger effects on decay time )
  - Addition of new decay modes:
    - $B_s \rightarrow J/\psi f^0$ , with  $f^0 \rightarrow \pi\pi$  ( less statistics but no angular analysis needed since final state is  $CP$  eigen-state)
    - $B_s \rightarrow \psi(2s)\phi$
  - Perform KK mass dependent fit (for more precise determination of s-wave contamination)
- Add more data !
  - 7 fb<sup>-1</sup> already recorded
  - expect to double sample size (~10 fb<sup>-1</sup>) by end of Tevatron running in 2011



## *Backup Slides*

# B Physics at the Tevatron

- Mechanisms for  $b$  production in  $p\bar{p}$  collisions at 1.96 TeV



- At Tevatron,  $b$  production cross section is much larger compared to B-factories
  - Tevatron experiments CDF and DØ enjoy rich B Physics program
- Plethora of states accessible only at Tevatron:  $B_s$ ,  $B_c$ ,  $\Lambda_b$ ,  $\Xi_b$ ,  $\Sigma_b$ ...
  - complement the B factories physics program
- Total inelastic cross section at Tevatron is  $\sim 1000$  larger than  $b$  cross section
  - large backgrounds suppressed by triggers that target specific decays

## $\beta_s$ vs $\phi_s$

- Up to now, introduced two **different** phases:

$$\phi_s^{\text{SM}} = \arg\left(-\frac{M_{12}}{\Gamma_{12}}\right) \approx 4 \times 10^{-3} \quad \text{and} \quad \beta_s^{\text{SM}} = \arg(-V_{ts}V_{tb}^*/V_{cs}V_{cb}^*) \approx 0.02$$

- New Physics affects both phases by **same** quantity  $\phi_s^{\text{NP}}$  (arxiv:0705.3802v2):

$$2\beta_s = 2\beta_s^{\text{SM}} - \phi_s^{\text{NP}}$$

$$\phi_s = \phi_s^{\text{SM}} + \phi_s^{\text{NP}}$$

- If the new physics phase  $\phi_s^{\text{NP}}$  dominates over the SM phases:  $2\beta_s^{\text{SM}}$  and  $\phi_s^{\text{SM}}$   
→ neglect SM phases and obtain:

$$2\beta_s = -\phi_s^{\text{NP}} = -\phi_s$$

# Decay Rate

-  $B_s \rightarrow J/\psi\phi$  decay rate (A.S. Dighe *et al.*, Phys. Lett. B **369** 144 (1996)) :

$$P_B(\theta, \phi, \psi, t) = \frac{9}{16\pi} |\mathbf{A}(t) \times \hat{n}|^2$$

where:  $\mathbf{A}(t) = (\mathcal{A}_0(t) \cos \psi, -\frac{\mathcal{A}_\parallel(t) \sin \psi}{\sqrt{2}}, i \frac{\mathcal{A}_\perp(t) \sin \psi}{\sqrt{2}})$  and  $\hat{n} = (\sin \theta \cos \phi, \sin \theta \sin \phi, \cos \theta)$

- Time evolution of transversity amplitudes  $A_0, A_\parallel, A_\perp$ :

$$A_i = \frac{e^{-\Gamma t/2}}{\sqrt{\tau_H + \tau_L \pm \cos 2\beta_s (\tau_L - \tau_H)}} [E_+(t) \pm e^{2i\beta_s} E_-(t)] a_i$$

where  $\pm$  corresponds to CP-even and CP-odd final states,  $\sum_i |a_i|^2 = 1$  and

$$E_\pm(t) \equiv \frac{1}{2} \left[ e^{+(\frac{-\Delta\Gamma}{4} + i\frac{\Delta m}{2})t} \pm e^{-(\frac{-\Delta\Gamma}{4} + i\frac{\Delta m}{2})t} \right]$$

- Finally:

$$\begin{aligned} P_B(\theta, \psi, \phi, t) &= \frac{9}{16\pi} \{ |\mathbf{A}_+(t) \times \hat{n}|^2 + |\mathbf{A}_-(t) \times \hat{n}|^2 + 2\text{Re}((\mathbf{A}_+(t) \times \hat{n}) \cdot (\mathbf{A}_-^*(t) \times \hat{n})) \} \\ &= \frac{9}{16\pi} \{ |\mathbf{A}_+ \times \hat{n}|^2 |f_+(t)|^2 + |\mathbf{A}_- \times \hat{n}|^2 |f_-(t)|^2 + 2\text{Re}((\mathbf{A}_+ \times \hat{n}) \cdot (\mathbf{A}_-^* \times \hat{n}) \cdot f_+(t) \cdot f_-^*(t)) \} \end{aligned}$$

$$|f_\pm(t)|^2 = \frac{1}{2} \frac{(1 \pm \cos 2\beta_s)e^{-\Gamma_L t} + (1 \mp \cos 2\beta_s)e^{-\Gamma_H t} \mp 2 \sin 2\beta_s e^{-\Gamma t} \sin \Delta m t}{\tau_L(1 \pm \cos 2\beta_s) + \tau_H(1 \mp \cos 2\beta_s)} \quad f_+(t)f_-^*(t) = \frac{e^{-\Gamma t} \cos \Delta m t + i \cos 2\beta_s e^{-\Gamma t} \sin \Delta m t + i \sin 2\beta_s (e^{-\Gamma_L t} - e^{-\Gamma_H t})/2}{\sqrt{[(\tau_L - \tau_H) \sin 2\beta_s]^2 + 4\tau_L \tau_H}}$$

## Decay Rate with S-Wave Included

- Including the s-wave contribution the probability density function becomes:

$$\rho_B(\theta, \phi, \psi, t, \mu) = \frac{9}{16\pi} \left| \left[ \sqrt{1 - F_s} g(\mu) \mathbf{A}(t) + e^{i\delta_s} \sqrt{F_s} \frac{h(\mu)}{\sqrt{3}} \mathbf{B}(t) \right] \times \hat{n} \right|^2$$

CP-odd

where:  $\mathbf{B}(t) = (B(t), 0, 0)$  and  $B(t) = \frac{e^{-\Gamma t/2}}{\sqrt{\tau_H + \tau_L - \cos 2\beta_s (\tau_L - \tau_H)}} [E_+(t) - e^{2i\beta_s} E_-(t)]$

$g(\mu)$  is relativistic Breit-Wigner to describe asymmetric  $\phi$  mass shape and  $h(\mu)$  is constant

- Integrating out the dependence on the KK mass:

$$\begin{aligned} \rho_B(\theta, \psi, \phi, t) &= (1 - F_s) \cdot P_B(\theta, \psi, \phi, t) + F_s Q_B(\theta, \psi, \phi, t) \\ &+ 2 \frac{\sqrt{27}}{16\pi} \text{Re} \left[ \mathcal{I}_\mu \left( (\mathbf{A}_- \times \hat{n}) \cdot (\mathbf{B} \times \hat{n}) \cdot |f_-(t)|^2 + (\mathbf{A}_+ \times \hat{n}) \cdot (\mathbf{B} \times \hat{n}) \cdot f_+(t) \cdot f_-^*(t) \right) \right] \end{aligned}$$

where:  $I(\mu)$  is a function of the s-wave phase and  $Q_B(\theta, \phi, \psi, t) = \frac{3}{16\pi} |\mathbf{B}(t) \times \hat{n}|^2$

# Analysis Improvements with Respect To 2008 Update

- Almost doubled data sample (from  $2.8 \text{ fb}^{-1}$  in 2008 to  $5.2 \text{ fb}^{-1}$  now)

- Improved signal selection:

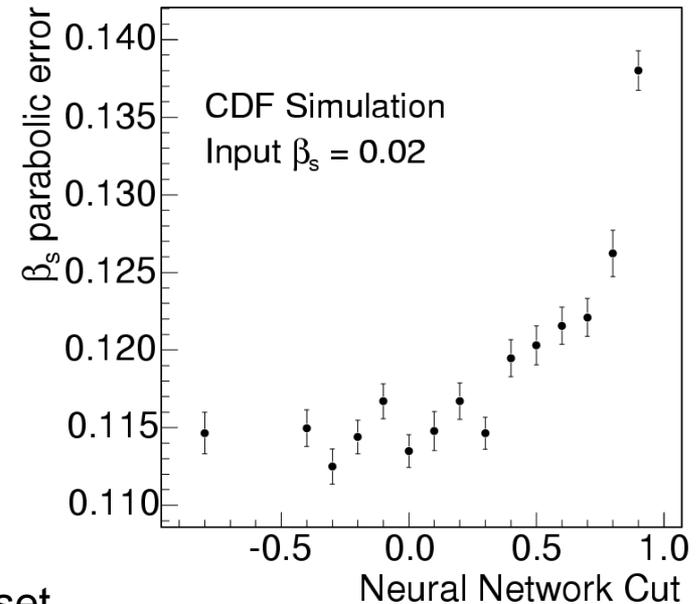
  - use particle ID (dE/dx and TOF) for full dataset

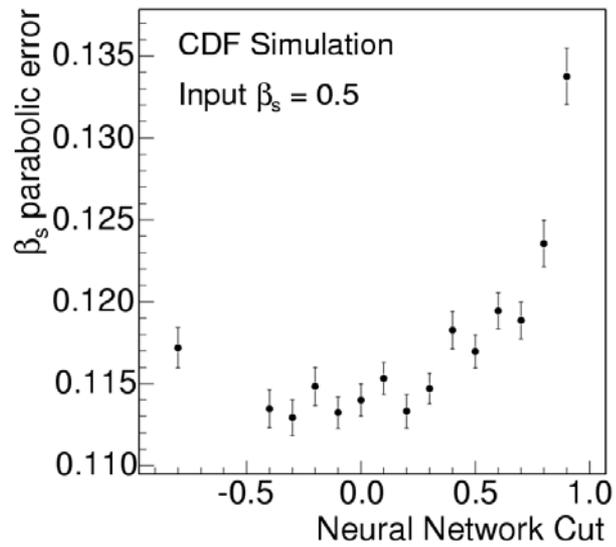
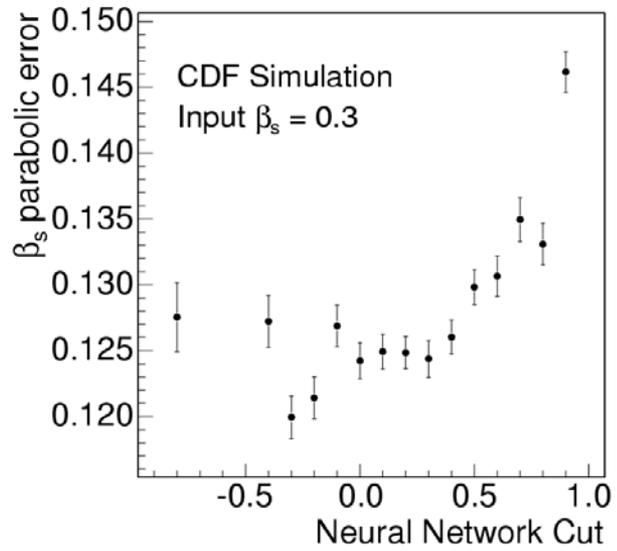
  - use pseudo-experiments to optimize neural network selection to minimize  $\beta_s$  statistical uncertainty (previously used  $S/(S+B)^{1/2}$  as figure of merit)

- Same side kaon tagger (SSKT) used for the full dataset

  - re-calibrated by measuring  $B_s$  mixing frequency with  $5.2 \text{ fb}^{-1}$

- Inclusion of S-wave contamination in the likelihood fit





# Comparison between tagged and un-tagged fit with and without accounting for S-wave

|  |   |
|--|---|
| $c\tau = 458.64 \pm 7.54$ (stat.) $\mu m$          | $c\tau = 459.1 \pm 7.7$ (stat.) $\mu m$           |
| $\Delta\Gamma = 0.075 \pm 0.035$ (stat.) $ps^{-1}$ | $\Delta\Gamma = 0.073 \pm 0.03$ (stat.) $ps^{-1}$ |
| $ A_{\parallel} ^2 = 0.231 \pm 0.014$ (stat.)      | $ A_{\parallel} ^2 = 0.232 \pm 0.014$ (stat.)     |
| $ A_0 ^2 = 0.524 \pm 0.013$ (stat.)                | $ A_0 ^2 = 0.523 \pm 0.012$ (stat.)               |
| $\phi_{\perp} = 2.95 \pm 0.64$ (stat.)             | $\phi_{\perp} = 2.80 \pm 0.56$                    |

Tagged, with S-wave

Tagged, no S-wave

Untagged, with S-wave

Untagged, no S-wave

|  |   |
|--|---|
| $c\tau = 456.93 \pm 7.69$ (stat.) $\mu m$          | $c\tau = 457.2 \pm 7.9$ (stat.) $\mu m$           |
| $\Delta\Gamma = 0.071 \pm 0.036$ (stat.) $ps^{-1}$ | $\Delta\Gamma = 0.070 \pm 0.04$ (stat.) $ps^{-1}$ |
| $ A_{\parallel} ^2 = 0.233 \pm 0.015$ (stat.)      | $ A_{\parallel} ^2 = 0.233 \pm 0.016$ (stat.)     |
| $ A_0 ^2 = 0.521 \pm 0.013$ (stat.)                | $ A_0 ^2 = 0.520 \pm 0.013$ (stat.)               |

## Systematic Uncertainties

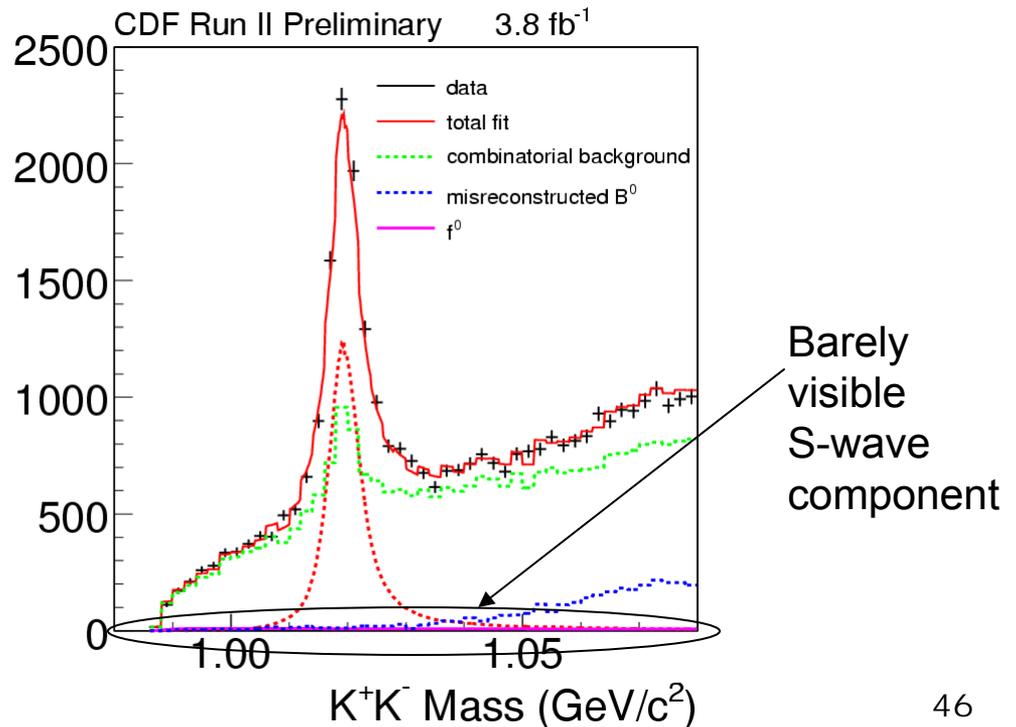
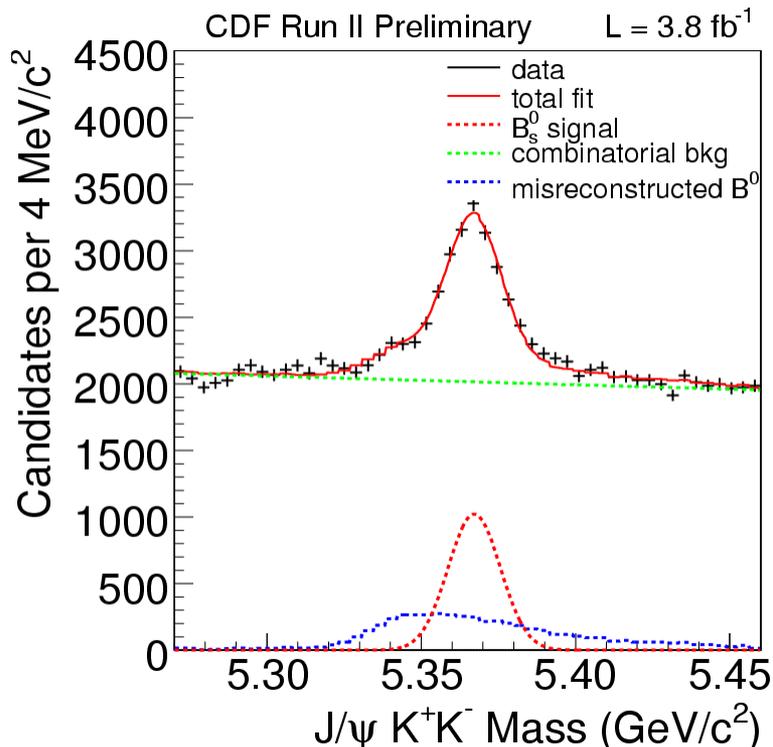
| Systematic                            | $\Delta\Gamma$ | $c\tau_s$  | $ A_{\parallel}(0) ^2$ | $ A_0(0) ^2$ | $\phi_{\perp}$ |
|---------------------------------------|----------------|------------|------------------------|--------------|----------------|
| Signal efficiency:                    |                |            |                        |              |                |
| Parameterisation                      | 0.0024         | 0.96       | 0.0076                 | 0.008        | 0.016          |
| MC reweighting                        | 0.0008         | 0.94       | 0.0129                 | 0.0129       | 0.022          |
| Signal mass model                     | 0.0013         | 0.26       | 0.0009                 | 0.0011       | 0.009          |
| Background mass model                 | 0.0009         | 1.4        | 0.0004                 | 0.0005       | 0.004          |
| Resolution model                      | 0.0004         | 0.69       | 0.0002                 | 0.0003       | 0.022          |
| Background lifetime model             | 0.0036         | 2.0        | 0.0007                 | 0.0011       | 0.058          |
| Background angular distribution:      |                |            |                        |              |                |
| Parameterisation                      | 0.0002         | 0.02       | 0.0001                 | 0.0001       | 0.001          |
| $\sigma(c\tau)$ correlation           | 0.0002         | 0.14       | 0.0007                 | 0.0007       | 0.006          |
| Non-factorisation                     | 0.0001         | 0.06       | 0.0004                 | 0.0004       | 0.003          |
| $B^0 \rightarrow J\psi K^*$ crossfeed | 0.0014         | 0.24       | 0.0007                 | 0.0010       | 0.006          |
| SVX alignment                         | 0.0006         | 2.0        | 0.0001                 | 0.0002       | 0.002          |
| Mass error                            | 0.0001         | 0.58       | 0.0004                 | 0.0004       | 0.002          |
| $c\tau$ error                         | 0.0012         | 0.17       | 0.0005                 | 0.0007       | 0.013          |
| Pull bias                             | 0.0028         |            | 0.0013                 | 0.0021       |                |
| <b>Totals</b>                         | <b>0.01</b>    | <b>3.6</b> | <b>0.015</b>           | <b>0.015</b> | <b>0.07</b>    |

## Dilution Scale Factor Systematic Uncertainties

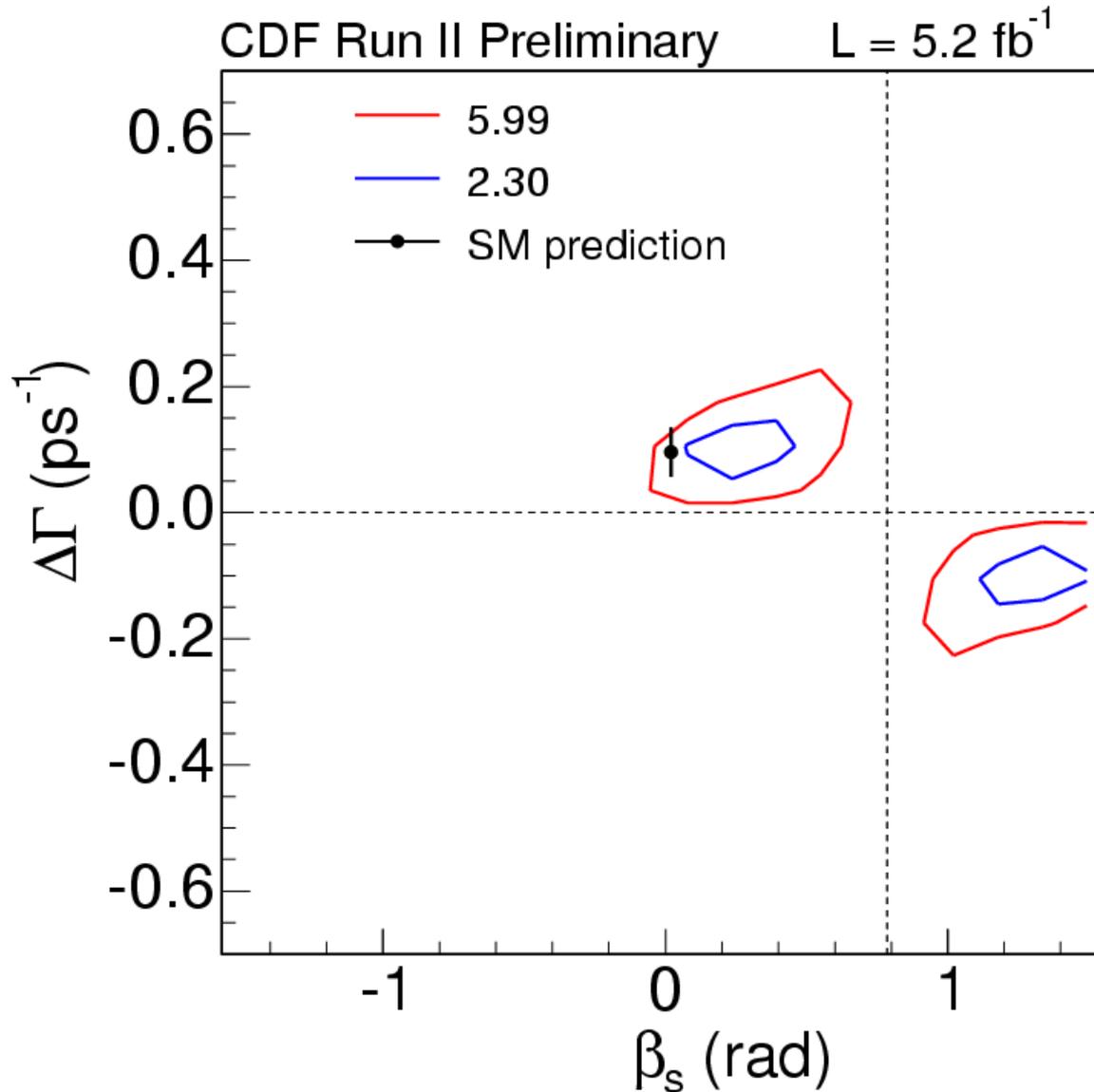
| Modification                         | Systematic Uncertainty |
|--------------------------------------|------------------------|
| Proper decay time resolution scaling | 0.11                   |
| Resolution model                     | 0.06                   |
| Cabibbo reflection                   | 0.03                   |
| Cabibbo fraction                     | negligible             |
| Mass window                          | negligible             |
| Selection of upper side band         | negligible             |
| $\Lambda_b$ template                 | negligible             |
| $\Delta\Gamma/\Gamma$                | negligible             |
| Mean Lifetime                        | negligible             |
| Trigger Composition                  | negligible             |
| Signal Mass Model                    | negligible             |
| <b>Total</b>                         | <b>0.13</b>            |

# S-Wave Cross Check Using KK Mass Spectrum

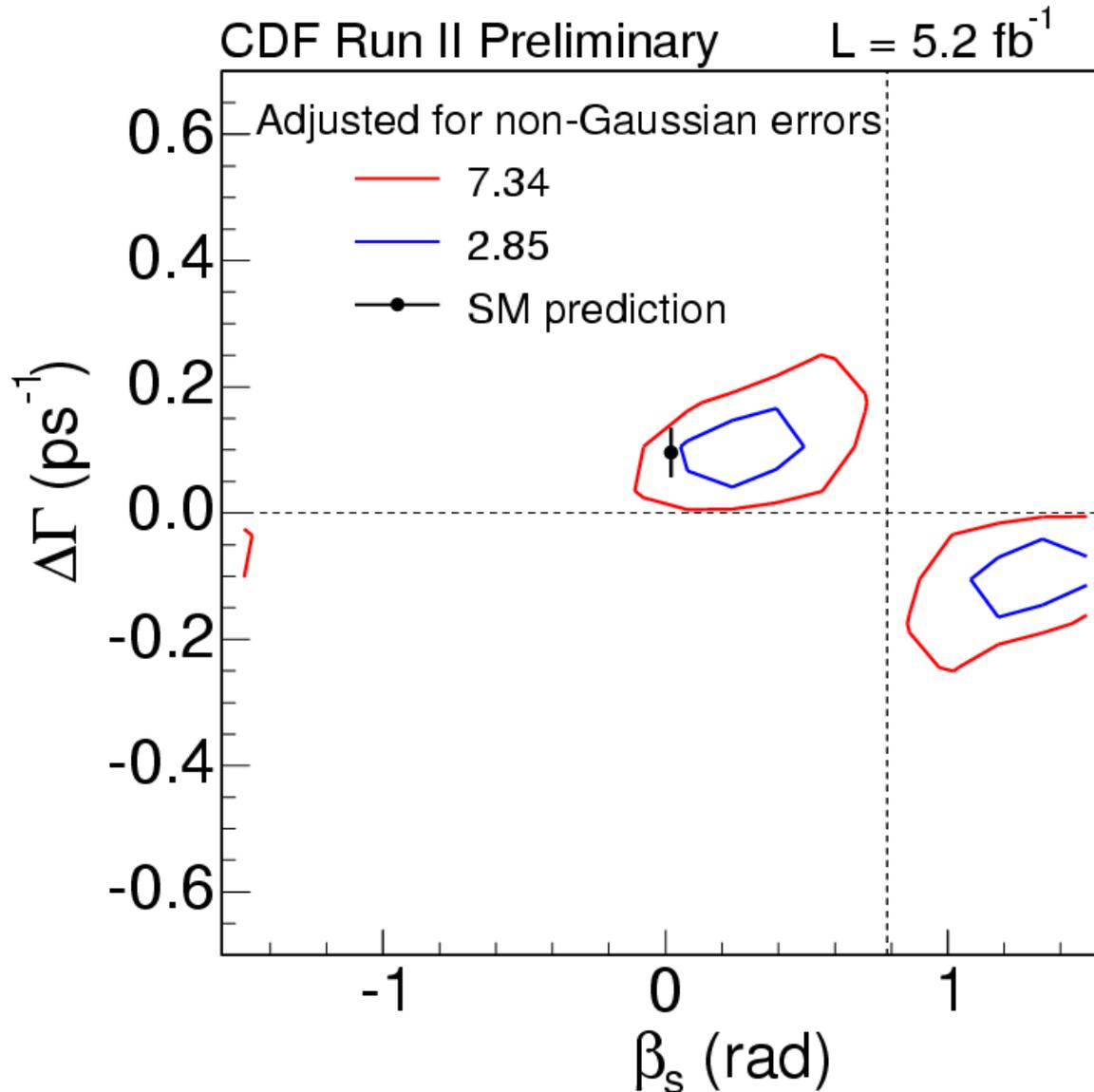
- Cross check the result from angular fit by fitting the KK invariant mass spectrum
- From a fit to the  $B_s$  mass distribution with wide KK mass range selection (0.980, 1.080 GeV), determine contributions of combinatorial background, mis-reconstructed  $B^0$ , and  $B_s$  events
- Good fit of the KK mass spectrum with 2%  $f^0$  contributions



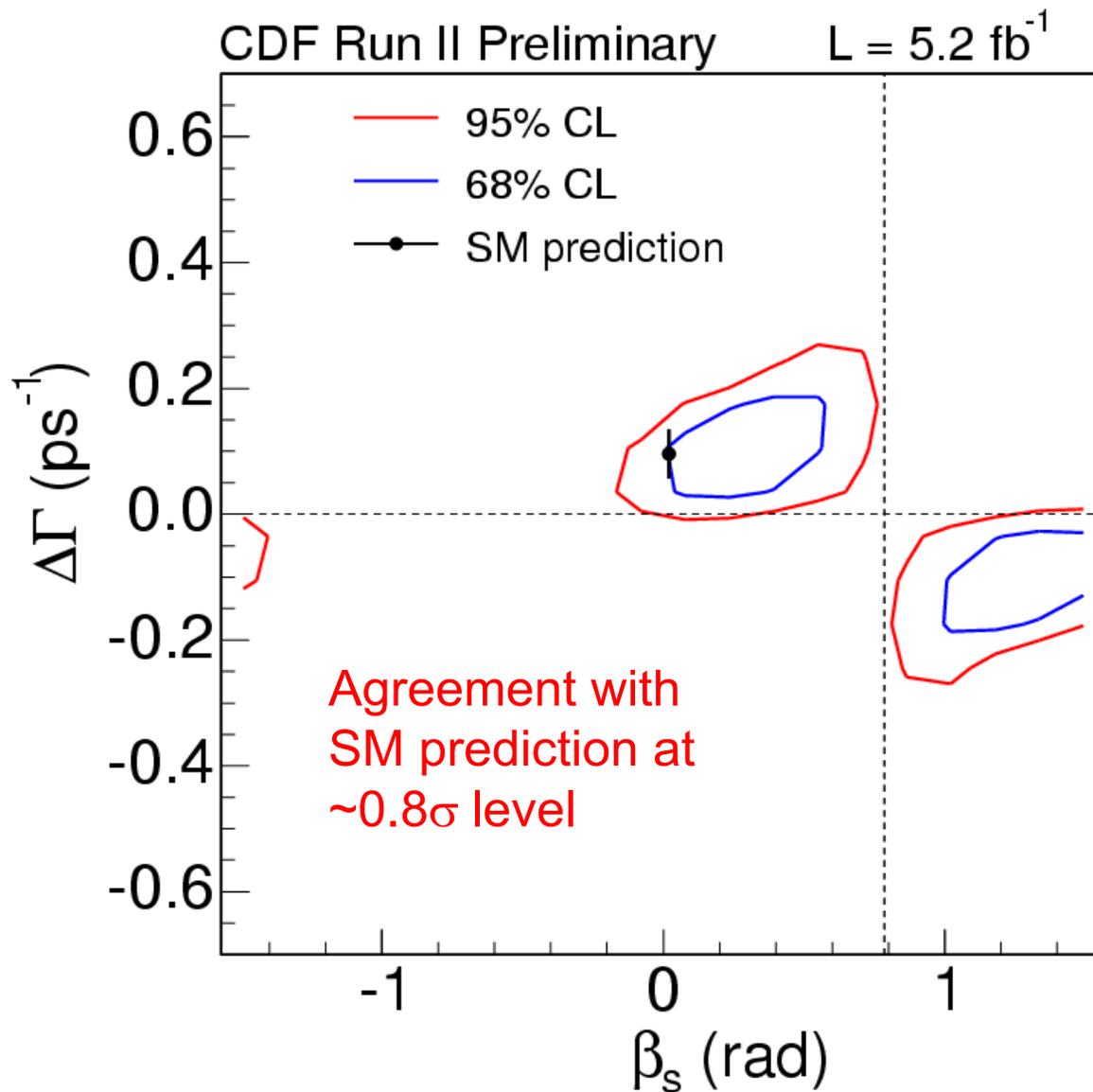
# $\beta_s$ - $\Delta\Gamma$ Contours Without Coverage Adjustment

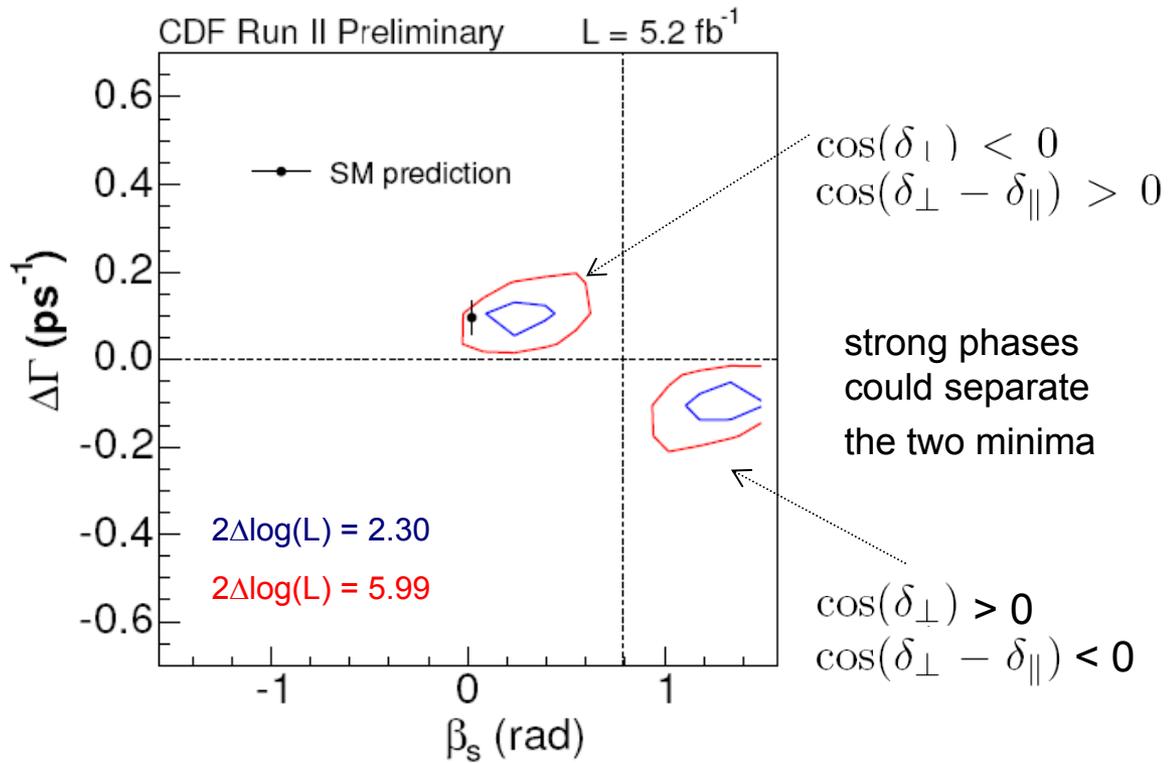


# $\beta_s$ - $\Delta\Gamma$ Contours With Coverage Adjustment



# $\beta_s$ - $\Delta\Gamma$ Contours With Systematics on Coverage





# Sensitivity

