

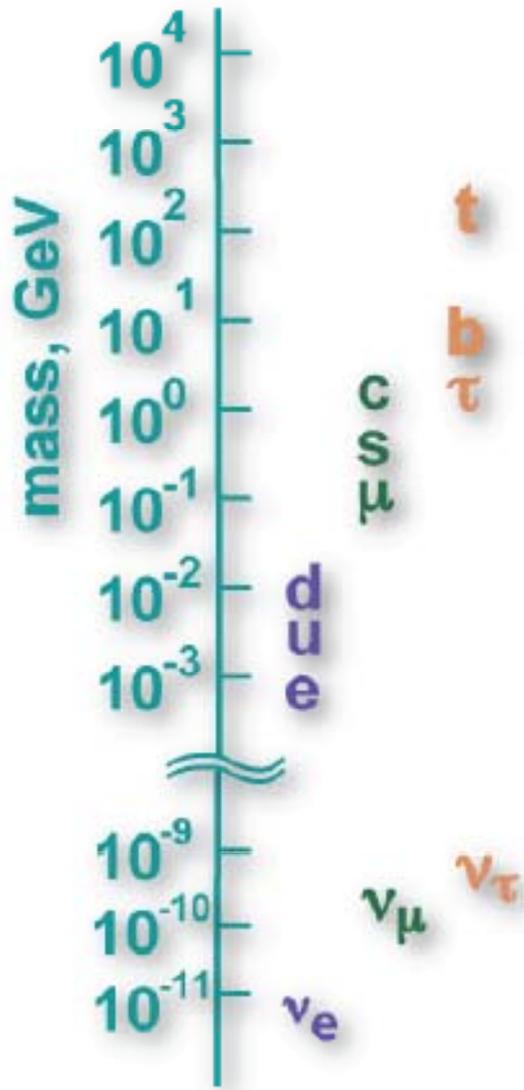


Top quark mass measurement at Tevatron

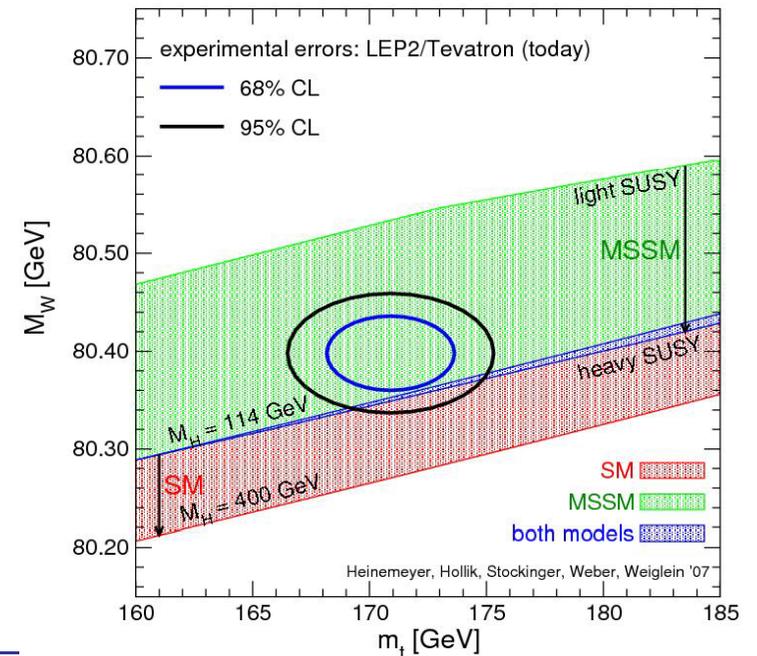
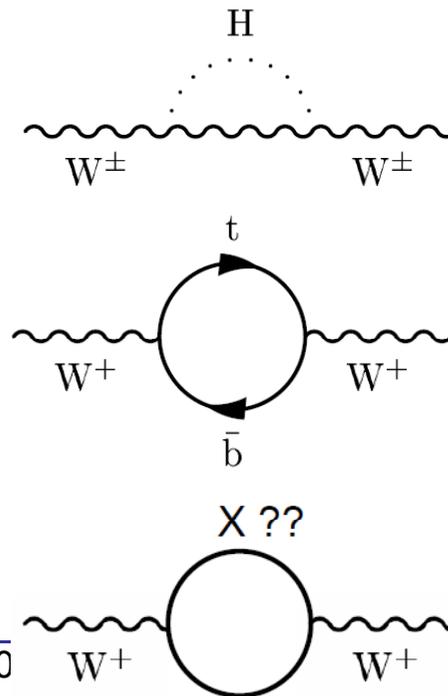
Hyunsu Lee
The University of Chicago

On behalf of the CDF and D0 collaboration

Top quark

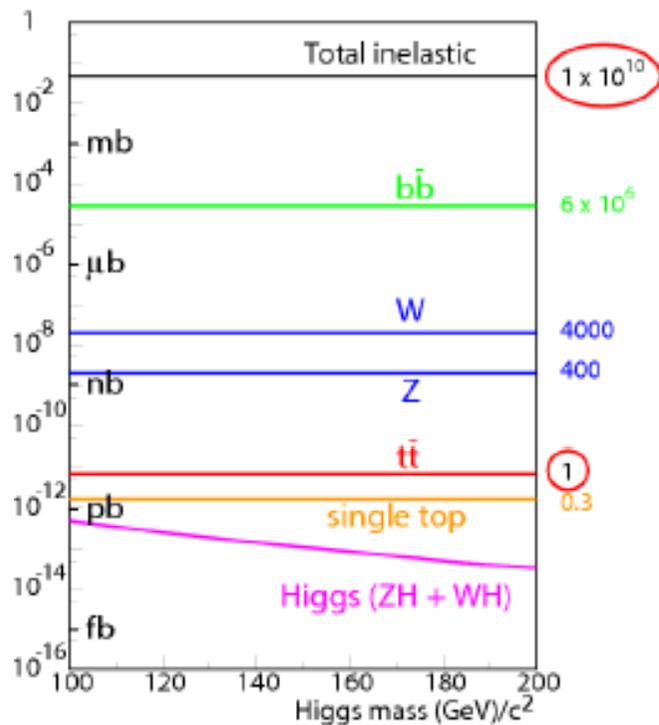
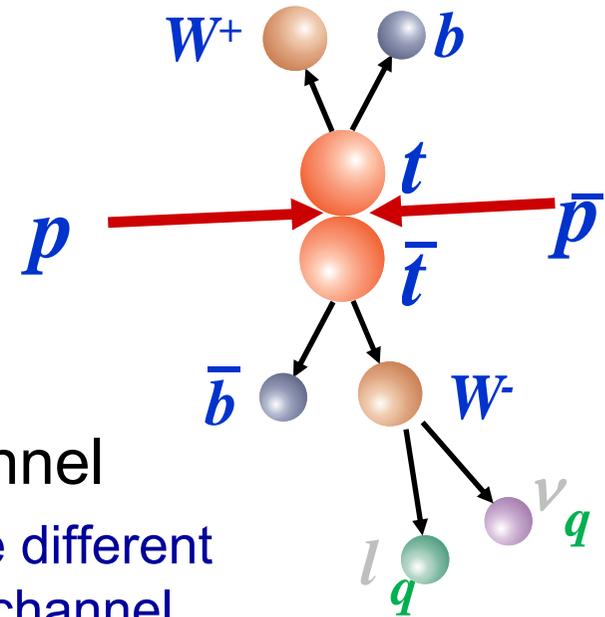


- Top quark is the heaviest known elementary particle
- Top quark mass is not predicted by SM
- Can constrain SM Higgs boson mass
 - ❖ Important contribution in radiative correction of W
 - ❖ Important test of SM



Top quark decay

- Pair production is predominated
- ~100% decay to W boson plus b quark
- Decay topologies rely on the decay of W boson
 - ❖ two jet (70%) or lepton and neutrino (30%)



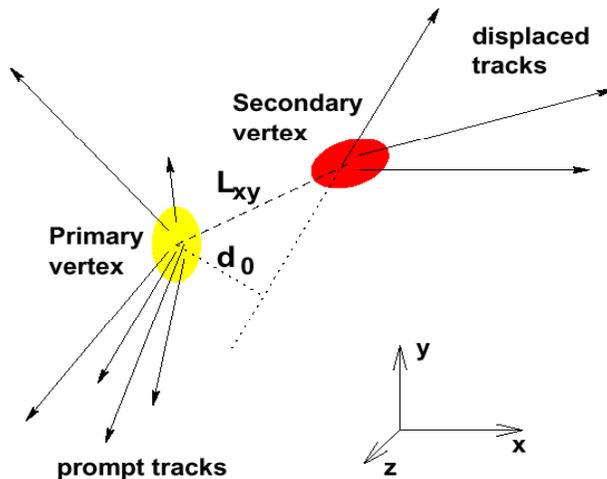
Important to look all channel

- ❖ New physics would make different phenomena for different channel

Challenge for mass measurement

- ❖ Up to six jet - Jet energy scale , jets to parton assignment
- ❖ Up to two neutrino – Missing energy – Event reconstruction
- ❖ Large QCD backgrounds

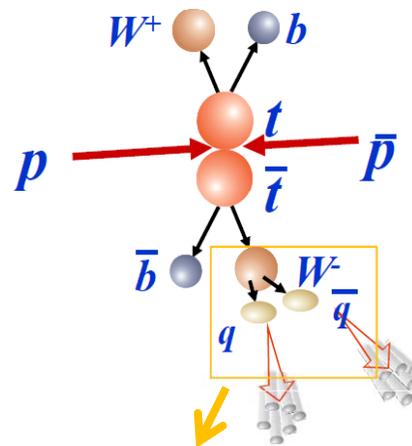
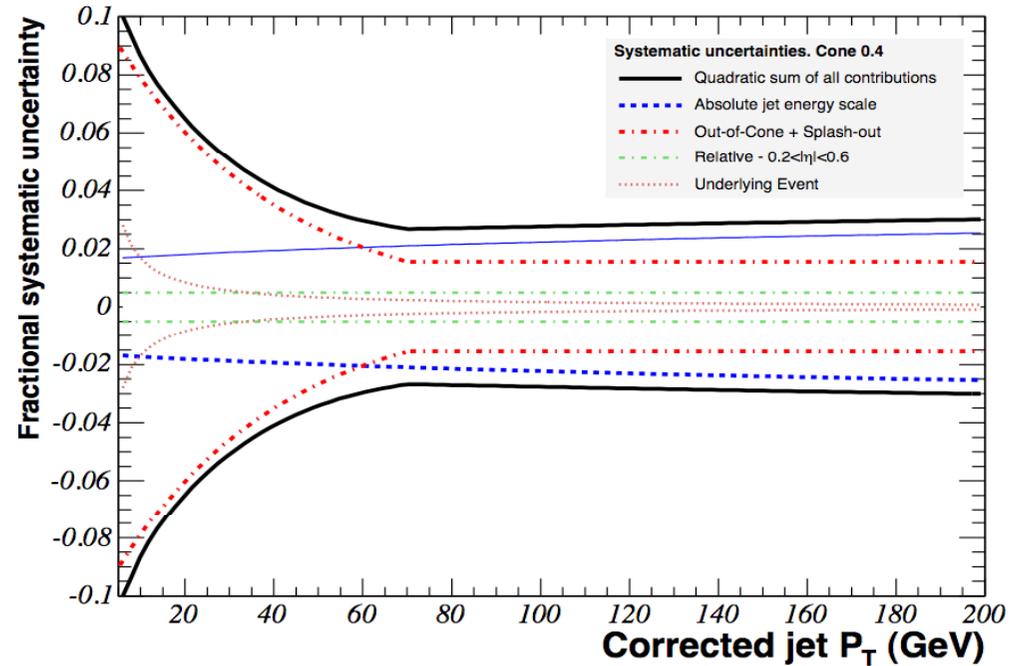
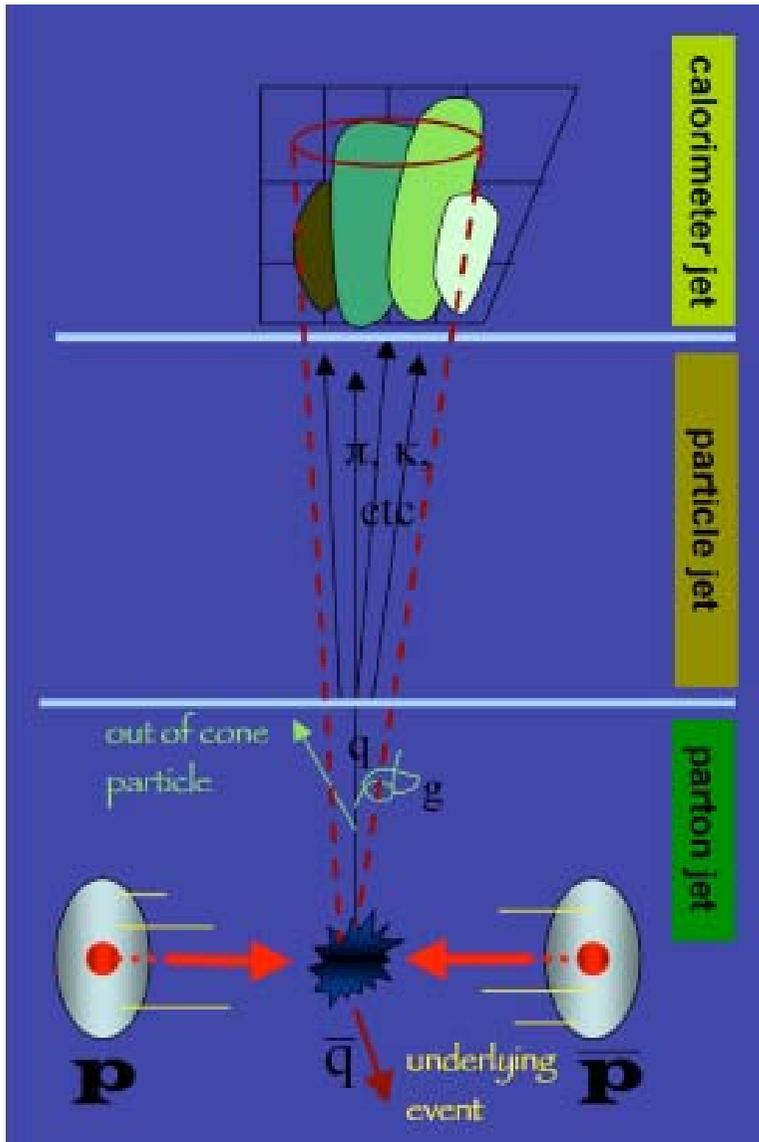
b-tagging



- B hadron can be identified by long displacement
- b tagging reduce # of jet-to-parton assign.
 - ❖ Ex) lepton+jets channel
 - ❖ 24 (0-btags), 6(1-btags), 2(2-btags)
- b tagging improve signal to background ratio significantly – 40% effi., 0.5% fake

Sample	Di-lepton (e, μ)	Lepton+jets (e, μ)	All Hadronic NN selection
0-b-tags S/B	1:1	1:4	1:20
1-b-tags S/B	4:1	4:1	1:5
2-b-tags S/B	20:1	20:1	1:1
Events in 1 fb^{-1} (≥ 1 b-tag)	25	180	150 (2 b-tags)

Jet energy scale



Measured JES uncertainty

Lepton+jets : $1.0 \text{ GeV}/c^2$

Dilepton : $2.9 \text{ GeV}/c^2$

(CDF 4.8 fb^{-1} , template method)

In situ JES calibration

Measurement technique (Matrix element technique)

- Try to extract as much information as possible from every event using theoretical prediction for ttbar production and decay
- Integrate over unknown parton energies given a measured jet energy
- For each event, we calculate probability to be ttbar with certain mass M_{top} (also JES)

**Transfer function between parton
and detector response**

$$P(\vec{x}; M_{top}, JES) \propto \int ME \times TF \times PDF$$

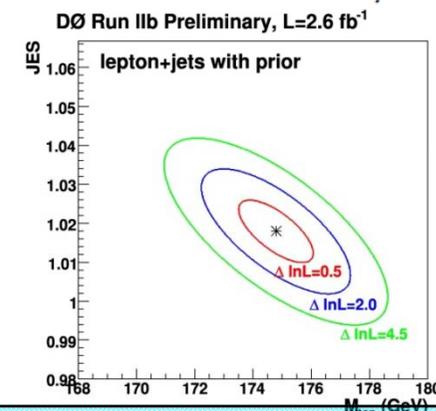
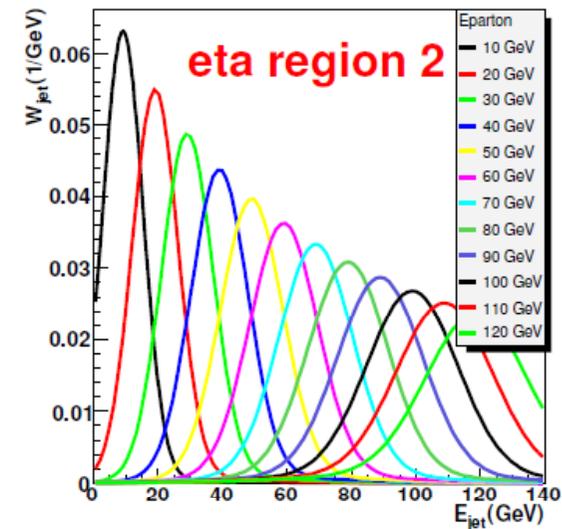
ttbar Matrix element **Parton distribution
function**

- Background probability is also calculated using background matrix element
- Perform the likelihood fit using event probability

D0 lepton+jets , ME



- 3.6 fb⁻¹ , 817 data events
- NN based b-tagging to increase efficiency
- Transfer function was estimated for four different eta region for b-jet, light jet, and lepton
- We modeled background only using W+jets ME
- 24 different permutations were summed by taking into account b-tagging information
- *In situ* JES calibration



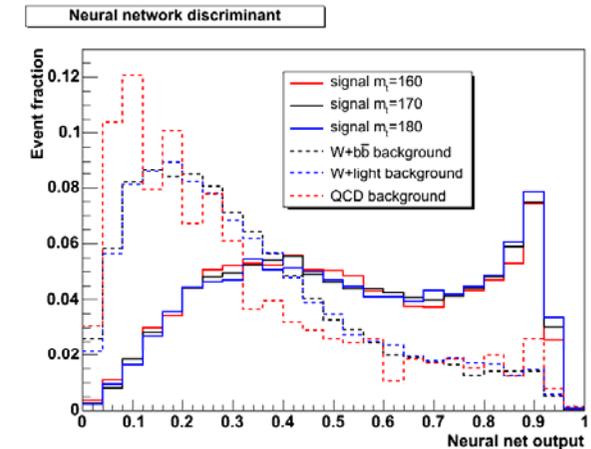
$$173.7 \pm 0.8 \text{ (stat)} \pm 1.6 \text{ (JES+syst)} \text{ GeV}/c^2$$
$$= 173.7 \pm 1.8 \text{ GeV}/c^2$$



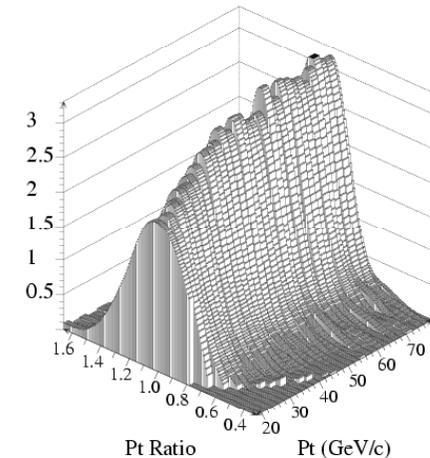
CDF lepton+jets, ME



- 4.8 fb⁻¹ data – 1070 events
 - ❖ We increase muon acceptance by adding MET+jets trigger (30% more events)
 - ❖ Additional NN based selection
- Transfer function was parameterized by eta and jet mass for b-jet and light jet
- *In situ* JES calibration
- This is the most precise top quark measurement to date



Transfer Function



$$172.8 \pm 0.7(\text{stat}) \pm 0.6(\text{JES}) \pm 0.8(\text{syst}) \text{ GeV}/c^2$$
$$= 172.8 \pm 1.3 \text{ GeV}/c^2$$



CDF lepton+jets, ME



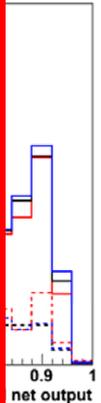
- 4.8 fb⁻¹

CDF Run II Preliminary, 4.8 fb⁻¹

- ❖ We
- ME
- ❖ Add

Systematic source	Systematic uncertainty (GeV/c ²)
Calibration	0.11
MC generator	0.25
ISR and FSR	0.15
Residual JES	0.49
<i>b</i> -JES	0.26
Lepton P_T	0.14
Multiple hadron interactions	0.10
PDFs	0.14
Background modeling	0.33
Gluon fraction	0.03
Color reconnection	0.37
Total	0.84

- Transf
- eta an
- *In situ*
- This is
- measu



Pt Ratio 0.4 20 Pt (GeV/c)

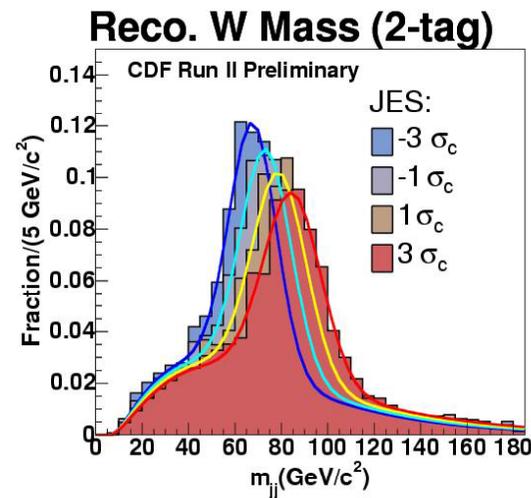
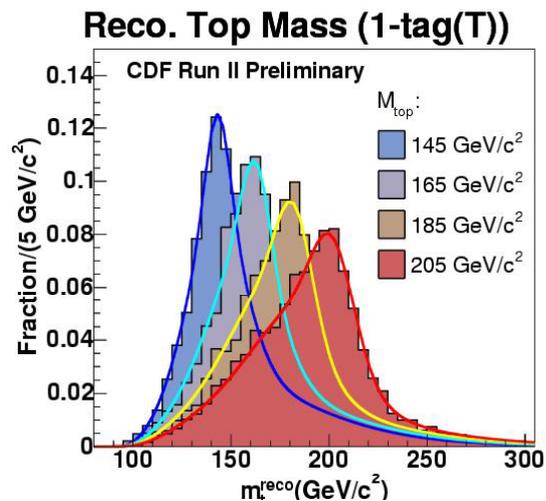


$$172.8 \pm 0.7(\text{stat}) \pm 0.6(\text{JES}) \pm 0.8(\text{syst}) \text{ GeV}/c^2$$

$$= 172.8 \pm 1.3 \text{ GeV}/c^2$$

Measurement technique (template method)

- Identify variables \vec{x} sensitive to M_{top} (or JES)
- Using MC, generate signal distribution of \vec{x} as a function of M_{top} (or JES)
- Parametrize templates in terms of probability density function then assign the probability for certain mass and JES



$$P(\vec{x}; M_{top}, \Delta JES)$$

Event reconstruction
in the lepton+jets

$$\chi^2 = \sum_{i=l,4jets} \frac{(p_T^{i,fit} - p_T^{i,meas})^2}{\sigma_i^2} + \sum_{j=x,y} \frac{(U_j^{fit} - U_j^{meas})^2}{\sigma_j^2} + \frac{(M_{jj} - M_W)^2}{\Gamma_W^2} + \frac{(M_{l\nu} - M_W)^2}{\Gamma_W^2} + \frac{(M_{bjj} - m_t^{reco})^2}{\Gamma_t^2} + \frac{(M_{bl\nu} - m_t^{reco})^2}{\Gamma_t^2}$$

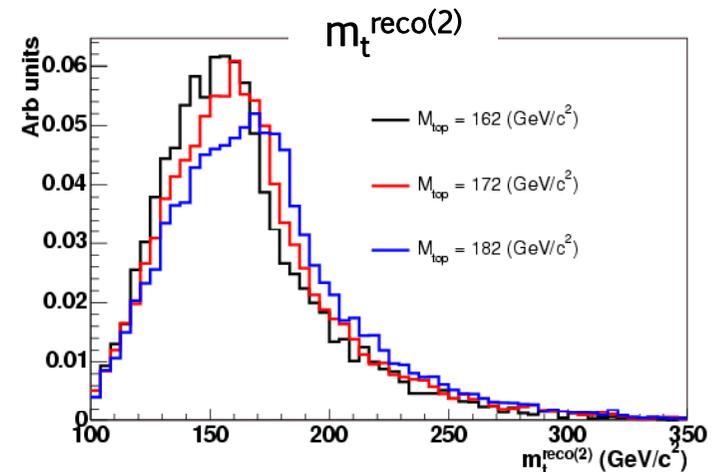
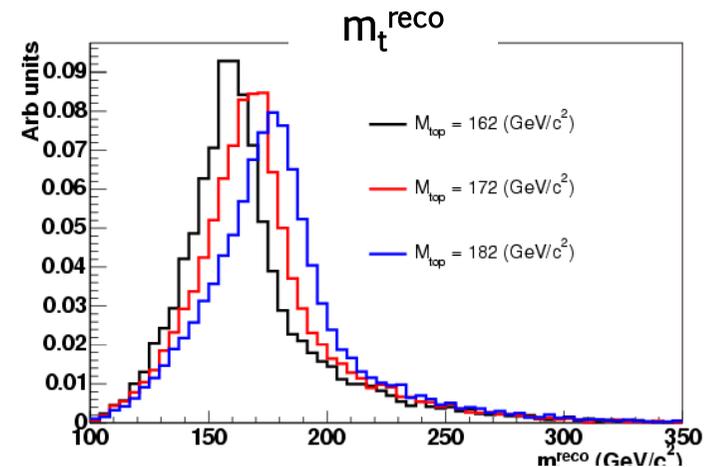
- Construct likelihood based on probabilities



CDF lepton+jets and dilepton, Template



- 4.8 fb⁻¹ data – 977 Lepton+jets(LJ)
344 Dilepton(DIL)
 - ❖ Chi2(<9) cut was applied for LJ
- Simultaneously use LJ+DIL
- Fully three dimensional PDF using three observables in LJ
 - ❖ 3rd observables is reconstructed mass using kinematic fit with different combinatoric of jet to parton assignment (2nd best fit)
- LJ only measurement
 - ❖ $172.0 \pm 1.5 \text{ GeV}/c^2$
 - ❖ Complement technique, consistent result



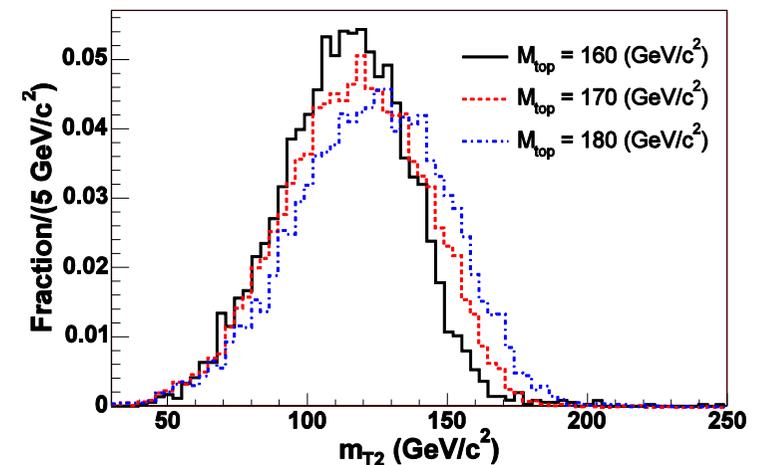
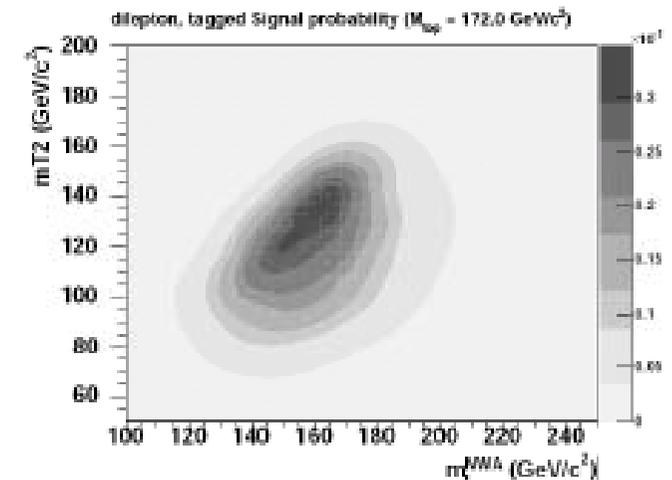
$$171.9 \pm 0.8 \text{ (stat)} \pm 0.8 \text{ (JES)} \pm 0.9 \text{ (syst)} \text{ GeV}/c^2$$
$$= 171.9 \pm 1.5 \text{ GeV}/c^2$$



CDF dilepton channel, template

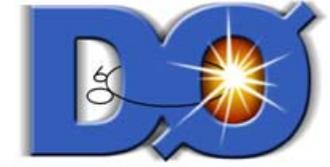


- Two observables taking into account correlation
 - ❖ Reconstructed mass and m_{T2}
- Interesting observable m_{T2}
 - ❖ Transverse mass with two missing particles
 - ❖ Introduced for mass measurement of New physics particles which have two missing particles
 - A. Barr *et. al.*, J.Phys.G 29 (2003) 2343
 - ❖ We firstly use m_{T2} in real data
 - Phys.Rev.D 81 (2010) 031102

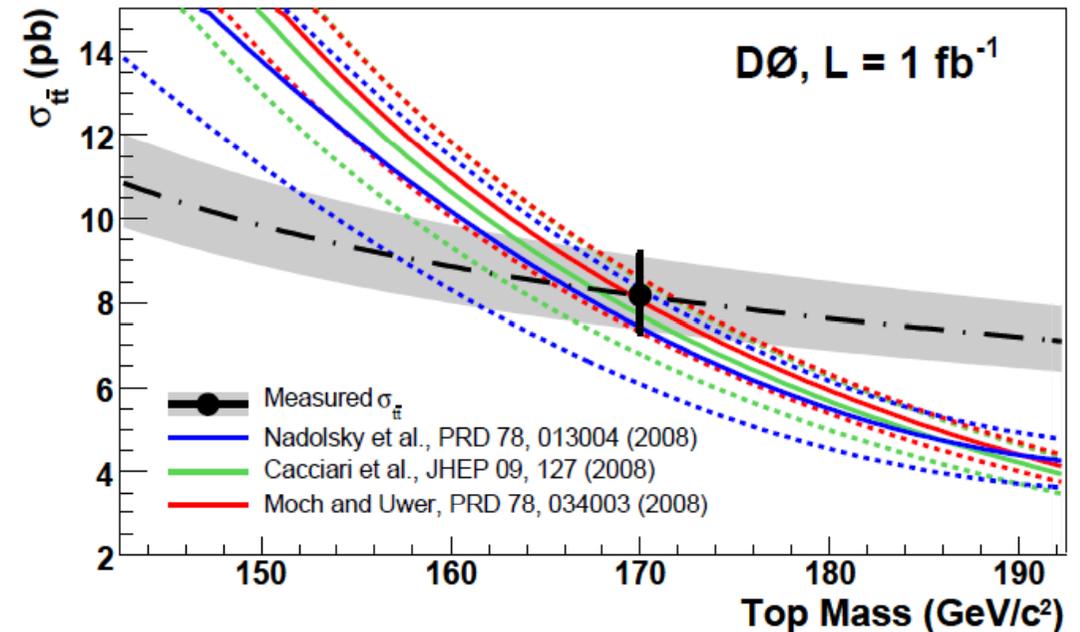


$$170.6 \pm 2.2 \text{ (stat)} \pm 3.1 \text{ (syst)} \text{ GeV}/c^2$$
$$= 170.6 \pm 3.8 \text{ GeV}/c^2$$

Top mass from cross section



- Top quark cross section measurement constraints top quark mass with taking into account theoretical calculation
PRD 80 (2009) 071102



NLO : $165.5^{+6.1}_{-5.9}$ (PRD 78 (2008) 013004)

NLO+NLL : $167.5^{+5.8}_{-5.6}$ (JHEP 09 (2008) 127)

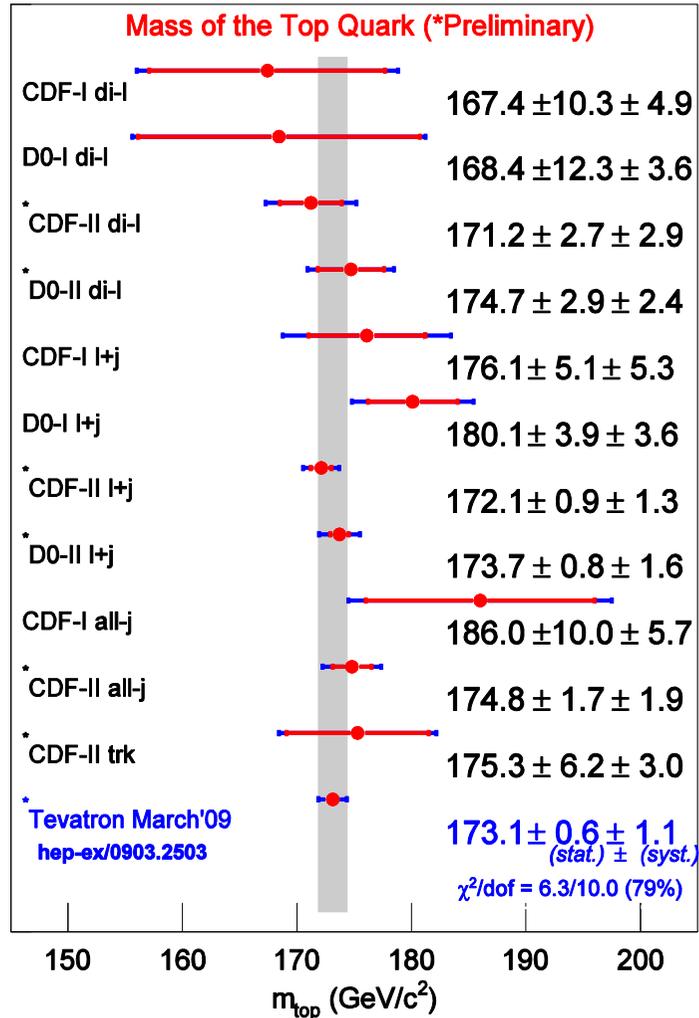
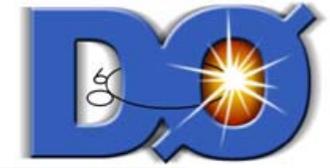
NLLO(approx.) : $169.1^{+5.9}_{-5.2}$ (PRD (2008) 074005)

NLLO (approx.) : $168.2^{+5.9}_{-5.4}$ (PLB 360 (1995) 47)

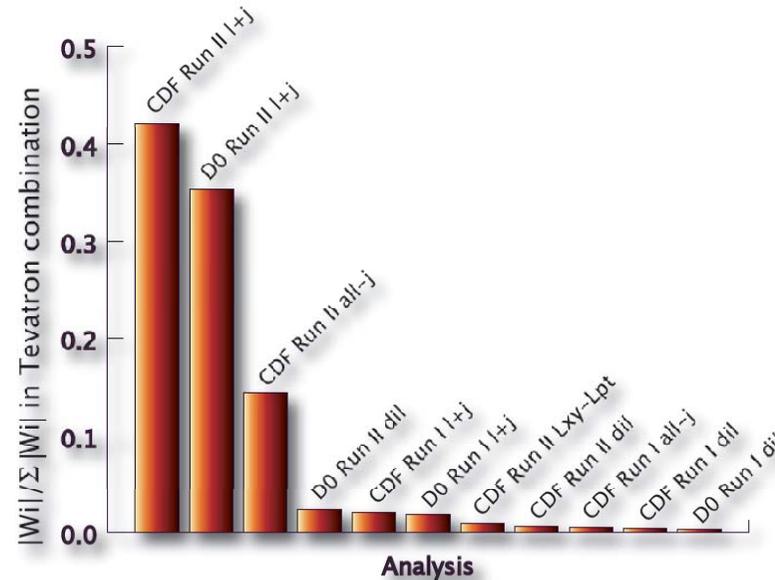
Complement technique, consistent result



Combination



$$m_{\text{top}} = 173.1 \pm 1.3 \text{ GeV}/c^2$$



New measurements

$$\text{CDF LJ (ME)} = 172.8 \pm 1.3 \text{ GeV}/c^2$$

$$\text{CDF LJ (TM)} = 172.1 \pm 1.5 \text{ GeV}/c^2$$

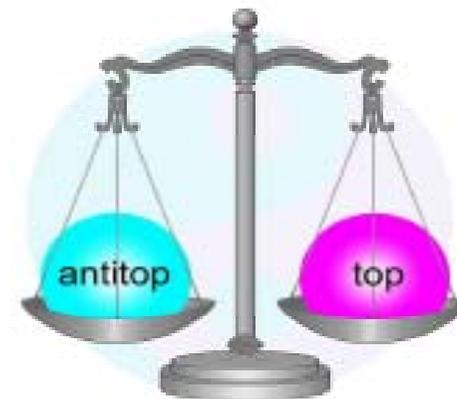
$$\text{CDF DIL(TM)} = 170.6 \pm 3.8 \text{ GeV}/c^2$$



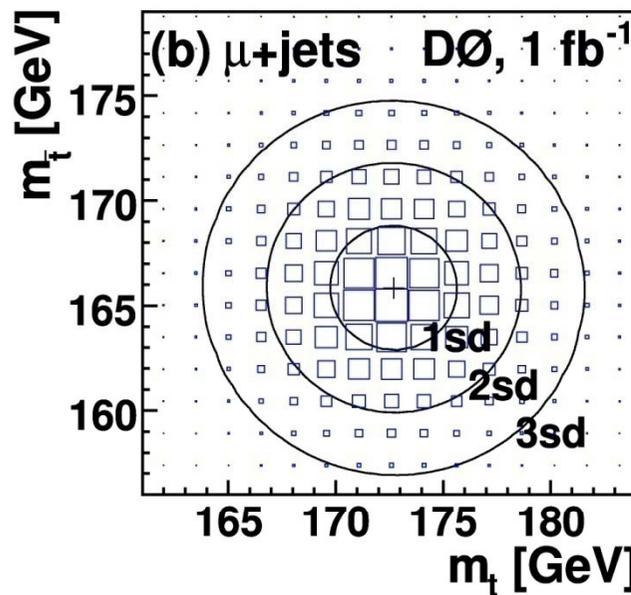
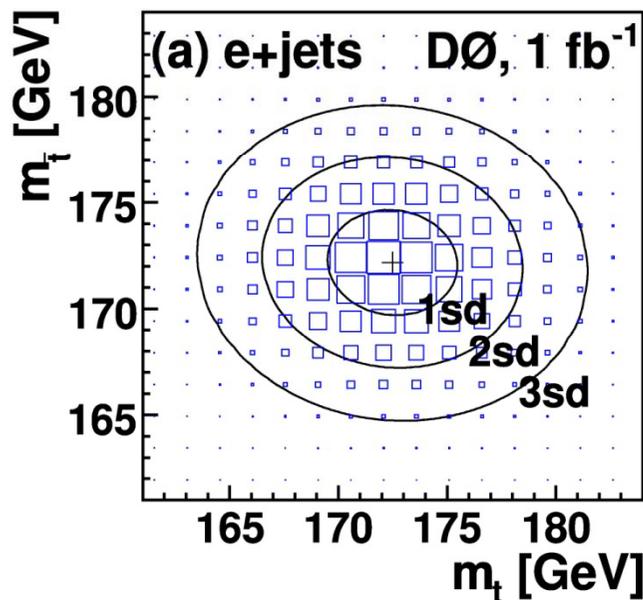
D0 top-antitop mass difference



- 1 fb⁻¹ modified matrix element
 - ❖ $P(\vec{x}; M_t, M_{\bar{t}})$ instead of $P(\vec{x}; M_{top}, JES)$
- **Test of CPT violation** in the top sector
 - ❖ First time in the quark and high mass



PRL 103 (2009) 132001



$$\Delta M = 3.8 \pm 3.7 \text{ GeV}/c^2$$

Good agreement with SM

Limited by statistics

Will be updated with more data



Conclusion



- 0.75% precision in world average (a year ago)

$$m_{\text{top}} = 173.1 \pm 1.3 \text{ GeV}/c^2$$

- 0.75% precision by single measurement (now)

$$m_{\text{top}} = 172.8 \pm 1.3 \text{ GeV}/c^2$$

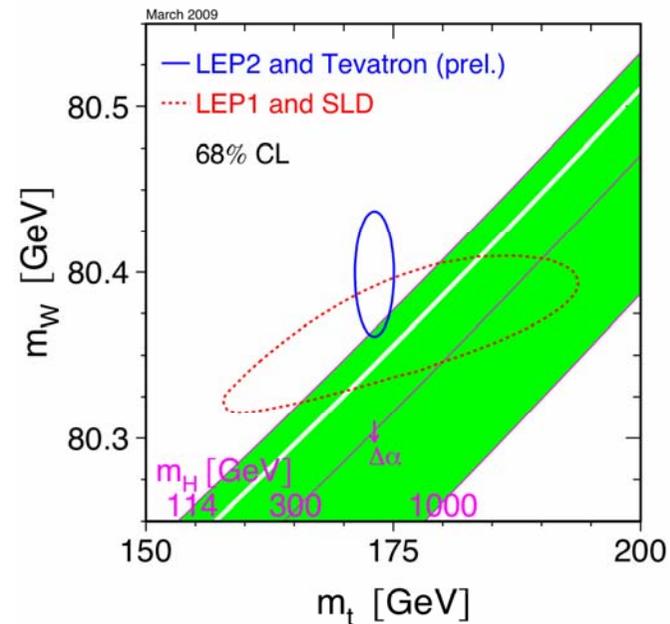
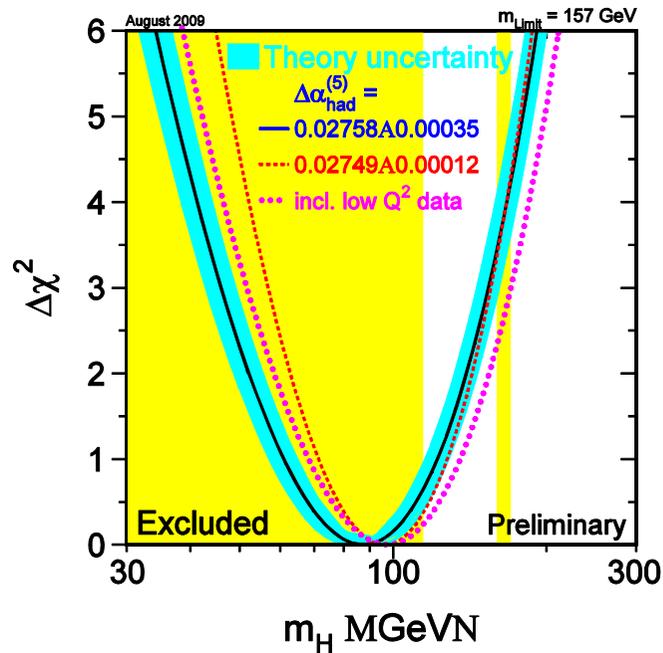
- We may have new measurement from LHC (next year)

- ❖ However Tevatron will have the most precise measurement for a while

Backup

Global EWK fit and Higgs constraints

LEPEWWG, arXiv:0911.2604 [hep-ex]



Not include new measurements

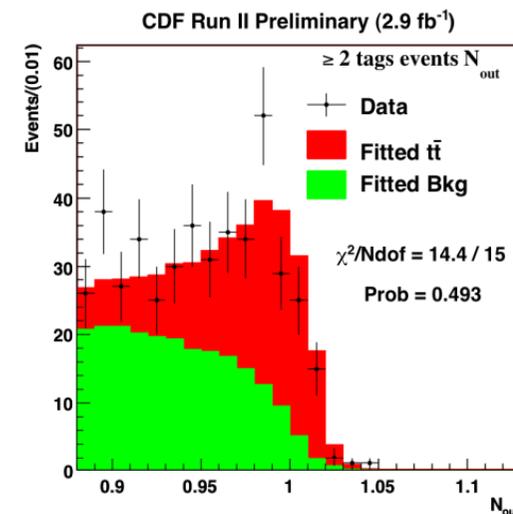
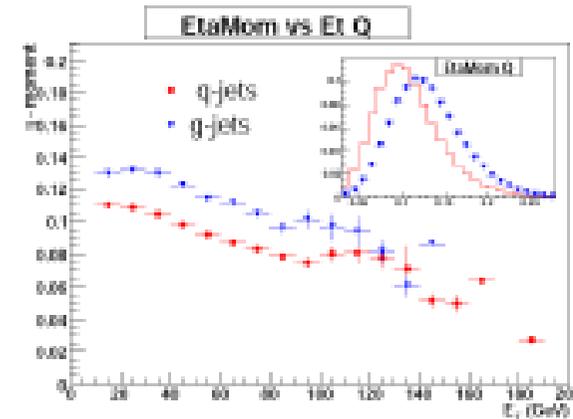
$$m_H = 87^{+35}_{-26} \text{ GeV}/c^2 \quad m_H < 157 \text{ GeV}/c^2 \text{ (95\% CL)}$$

$$m_H < 187 \text{ GeV}/c^2 \text{ (95\% CL)}$$

With direct limit from LEP II

CDF all hadronic channel

- 2.9 fb⁻¹ data, template method
- Two dimensional template
 - ❖ Reconstructed top mass and dijet mass from W boson decay
- NN discrimination to reduce dominant QCD backgrounds
 - ❖ Jet shape to discriminate gluon jet from quark jet
 - ❖ 1btag S:B=1:4 (3452 candidates)
 - ❖ 2btag S:B=1:1 (441 candidates)

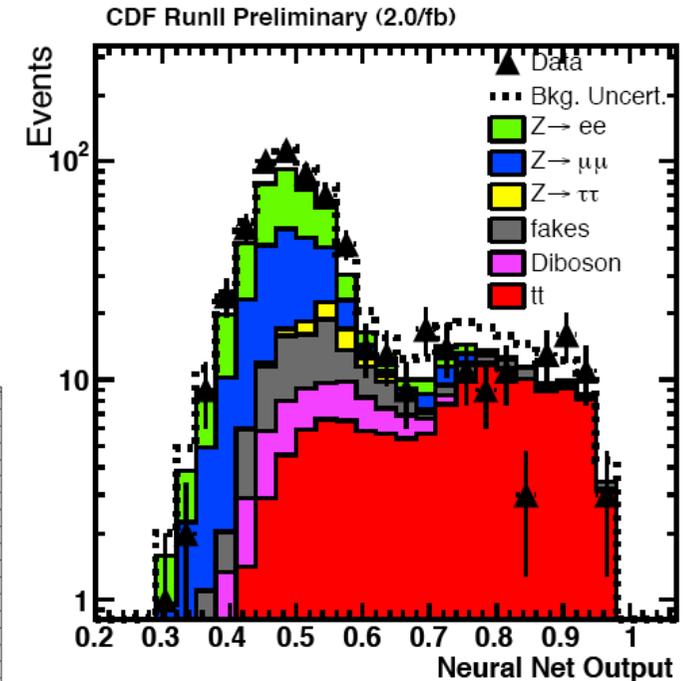
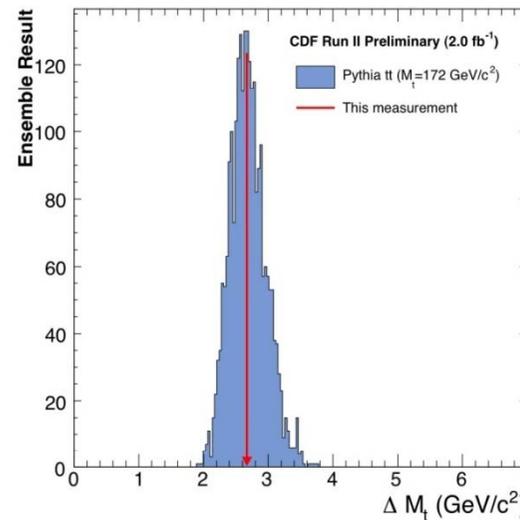
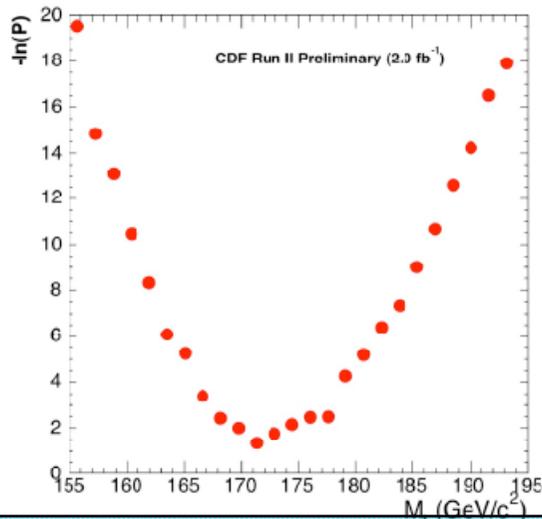


$$174.8 \pm 1.7 \text{ (stat)} \pm 1.9 \text{ (JES+syst)} \text{ GeV}/c^2$$

$$= 174.8 \pm 2.7 \text{ GeV}/c^2$$

CDF dilepton channel, ME

- 2.0 fb⁻¹ data, Matrix element method
- Event selection was optimized for top quark mass measurement using NN
- More sensitive analysis than template method



$$171.2 \pm 2.7 \text{ (stat)} \pm 2.9 \text{ (syst)} \text{ GeV}/c^2$$

$$= 171.2 \pm 4.0 \text{ GeV}/c^2$$

D0 dilepton channel



- We have two b-jets, two lepton, and two neutrino
 - ❖ Underconstraint system

- Event reconstruction to build template is challenging

Neutrino weighting

Integrate over expected neutrino eta distribution to obtain a probability for certain top mass

Matrix weighting

- 1.0 fb^{-1} , template method
 - ❖ $174.7 \pm 4.4(\text{stat}) \pm 2.0(\text{syst}) \text{ GeV}/c^2$

- Matrix element calculation
 - Integrate over unknown neutrino momentum

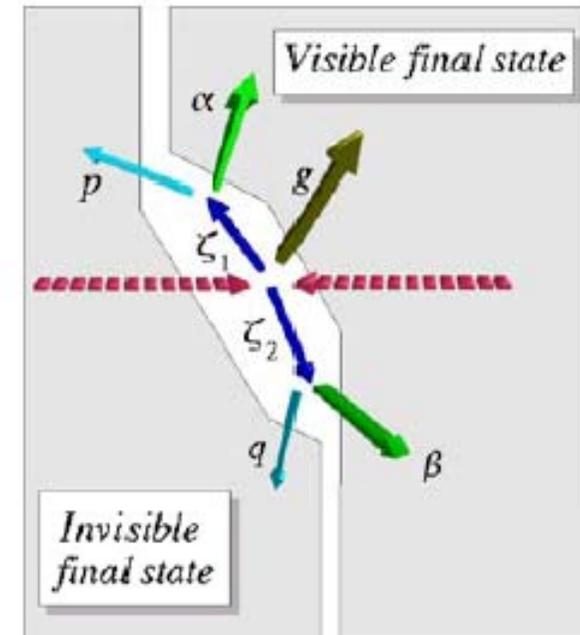
- We use Z to tau tau +jets for background modeling

- 3.6 fb^{-1} , ME, Only use eμ events
 - ❖ $174.8 \pm 3.3(\text{stat}) \pm 2.6(\text{syst}) \text{ GeV}/c^2$

$$174.7 \pm 2.9 (\text{stat}) \pm 2.4 (\text{syst}) \text{ GeV}/c^2 \\ = 174.7 \pm 3.8 \text{ GeV}/c^2$$

m_{T2}

- Introduced to measure the mass of new physics particle)
 - ❖ Most of new physics predict long-live stable particle – dark matter candidate
 - ❖ We expect missing particle at the final state
 - ❖ If we consider pair production of new physics particle, it will have two missing particle



- Top dilepton channel have exactly same final state

$$m_{T2} = \min[\max(m_{T(1)}, m_{T(2)})]$$

$$\mathbf{q}_T + \mathbf{p}_T = \text{missing } \mathbf{p}_T$$

Alan Barr, Christopher Lester and Phil Stephens
J. Phys. G: Nucl. Part. Phys. 29 (2003) 2343–2363

- Leptonical decay of top

- ❖ $t \rightarrow b \ell \nu$

- ❖ We measure b and lepton but don't know neutrino

- 4 unknown

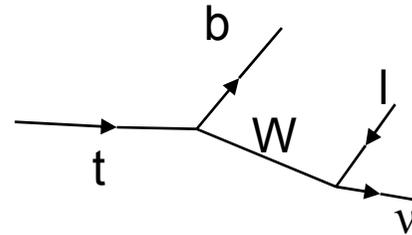
- ❖ Known parameter

- W mass, neutrino mass (2 unknown)

- ❖ If we assume the top quark mass and neutrino eta direction, we can measure neutrino x,y momentum

- ❖ Same thing happen for the other leg

- Getting weight using measured missing transverse energy



$$B \equiv 2b\nu = m_t^2 - m_W^2 - m_b^2 - 2b\ell$$

$$L \equiv 2\ell\nu = m_W^2 - m_\ell^2 - m_\nu^2$$

$$= m_W^2 - m_\ell^2$$

$$w_i = \exp\left(-\frac{(\cancel{E}_x - P_x^\nu - P_x^\bar{\nu})^2}{2\sigma_x^2}\right) \cdot \exp\left(-\frac{(\cancel{E}_y - P_y^\nu - P_y^\bar{\nu})^2}{2\sigma_y^2}\right)$$

$$w_i = w_i(m_{top}, \eta_1^\nu, \eta_2^\nu)$$

m_t^{NWA}

- Some over neutrino rapidities

$$W(m_t) = \int d\eta_1 \int d\eta_2 P(\eta_1) P(\eta_2) \sum_j \sum_i w(m_t)_{i,j}$$

- We have maximum weight m_t as reconstructed mass (m_t^{NWA})
- We scan m_t with 3GeV size and then decrease the step size upto 0.15GeV near the peak
- We have gaussian fit in the near of peak to get m_t continuously

